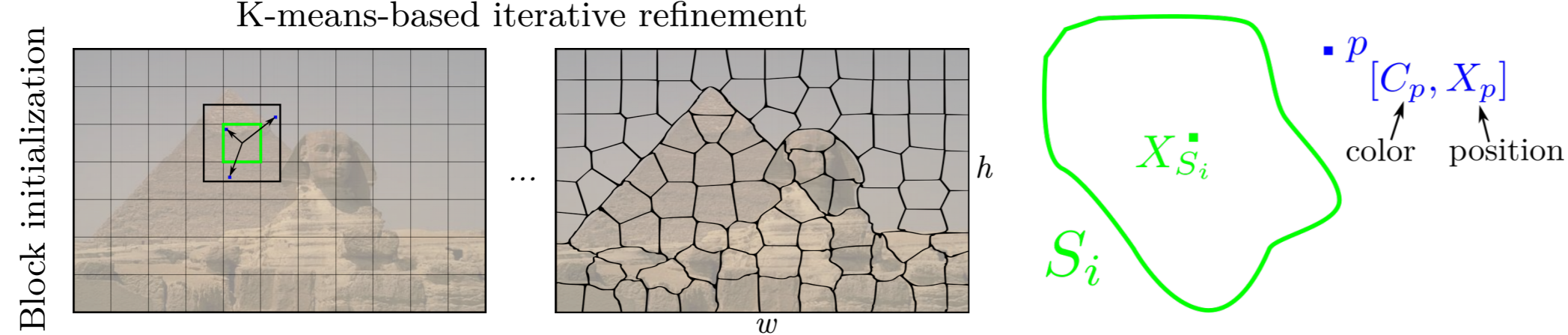


## Abstract

Most of existing superpixel methods are designed to segment standard planar images as pre-processing for computer vision pipelines. Nevertheless, the increasing number of applications based on wide angle capture devices, mainly generating 360° spherical images, have enforced the need for dedicated superpixel approaches. In this paper, we introduce a new superpixel method for spherical images called SphSPS (for Spherical Shortest Path-based Superpixels). Our approach respects the spherical geometry and generalizes the notion of shortest path between a pixel and a superpixel center on the 3D spherical acquisition space. To relevantly evaluate this last aspect in the spherical space, we also generalize a planar global regularity metric. Finally, the proposed SphSPS method obtains significantly better performances than both planar and spherical recent superpixel approaches on the reference 360° spherical panorama segmentation dataset.

## Spherical Superpixels based on SLIC [1]

### • SLIC (Simple Linear Iterative Clustering) [2]:



$$D_{SLIC}(p, S_i) = d_{color}(C_p, C_{S_i}) + d_{spatial}(X_p^a, X_{S_i}^a)$$

### • Adaptation to spherical geometry SphSLIC [1]:

- Search area: Regular in the acquisition (spherical) space



- Distance  $d_{spatial} = \|X_p^a - X_{S_i}^a\|_2^2$  on spherical coordinates  $X^a$ :

$$X^a = \begin{cases} x^a = \sin(\frac{y^a}{h}) \cos(\frac{2x^a\pi}{w}) \\ y^a = \sin(\frac{y^a}{h}) \sin(\frac{2x^a\pi}{w}) \\ z^a = \cos(\frac{y^a}{h}) \end{cases} \leftrightarrow X = \begin{cases} x = \frac{\arctan2(y^a, x^a)w}{2\pi} \\ y = \frac{\arccos(z^a)h}{\pi} \end{cases}$$

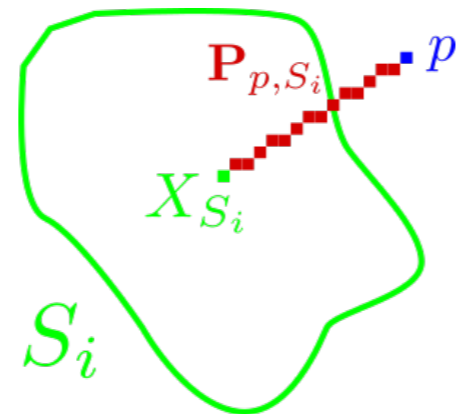
→ Same SLIC limitations: non-robustness to noise, irregular shapes, poor contour adherence, ...

## Spherical Shortest Path-based Superpixels (SphSPS)

### • Shortest path-based distance:

SCALP (Superpixels with Contour Adherence using Linear Path) [3]

- Color distance of each pixel in linear path  $\mathbf{P}_{p, S_i}$  to the barycenter of the superpixel → Robustness to noise + regular shapes
- Maximum of contour map intensity on  $\mathbf{P}_{p, S_i}$  → Respect of object contours



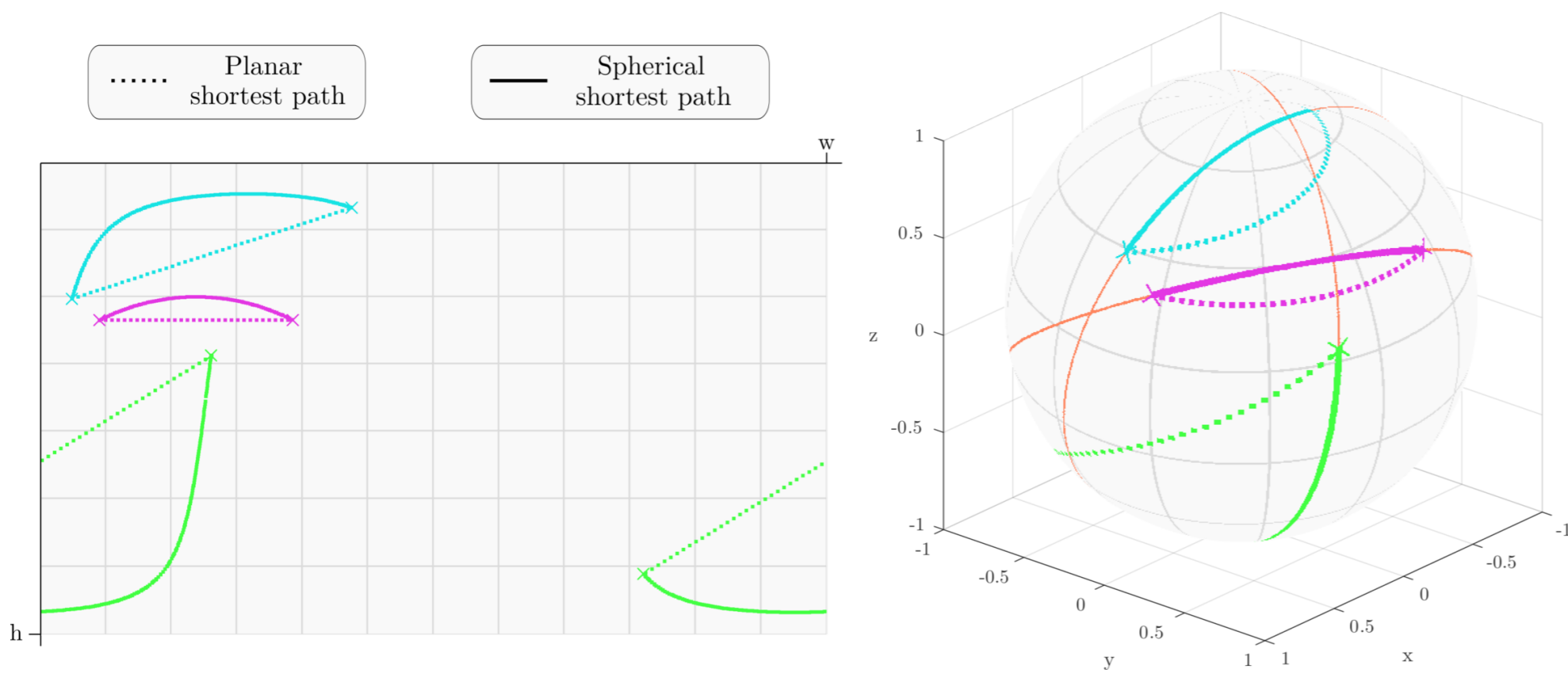
$$D_{SPS}(p, S_i) = (d_{color}(C_p, C_{S_i}, \mathbf{P}_{p, S_i}) + d_{spatial}(X_p, X_{S_i})) d_{contour}(\mathbf{P}_{p, S_i})$$

### • Generalized shortest path:

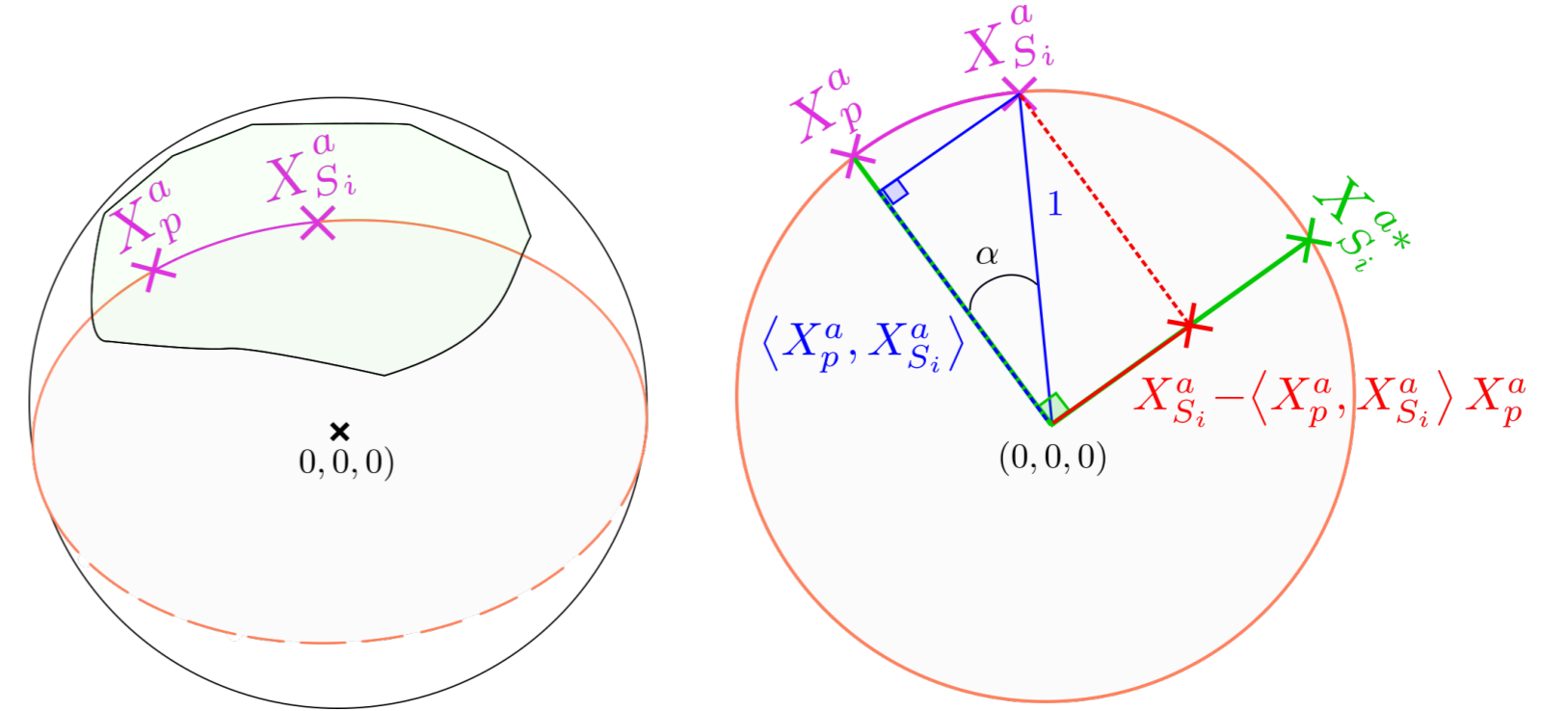
$$\mathbf{P}_{p, S_i} = \mathbf{P}_{p, S_i}^a \xrightarrow{\text{proj}} \{\mathbb{N}^2\} \quad \begin{matrix} \mathbf{P}_{p, S_i} & \text{Path in planar space} \\ \mathbf{P}_{p, S_i}^a & \text{Shortest Path in acquisition space} \end{matrix}$$

### • Spherical acquisition space:

The shortest path  $\mathbf{P}_{p, S_i}^a$  follows the geodesic along the great circle (containing the two points and the sphere center)



- Fast discrete implementation:  $N$  sampled points on the great circle



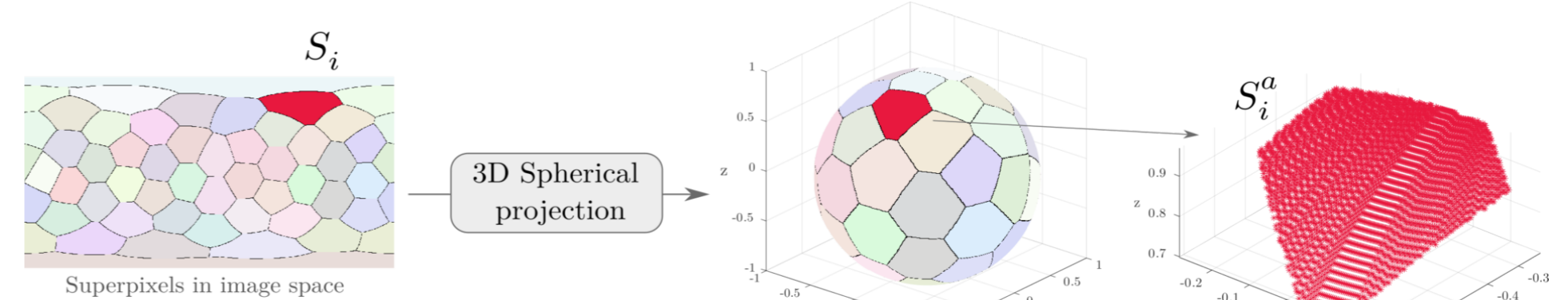
$$\mathbf{P}_{p, S_i}^a = \cos(\alpha_N) X_p^a + \sin(\alpha_N) X_{S_i}^{a*} \quad \text{with } \alpha_N = \frac{[0, N-1]}{N-1} \alpha \in \mathbb{R}^N$$

- Recursive optimization using path redundancy:

→ SphSPS runs in 0.7s for 1024x512 images (SphSLIC [2]  $\approx$  2.5s)

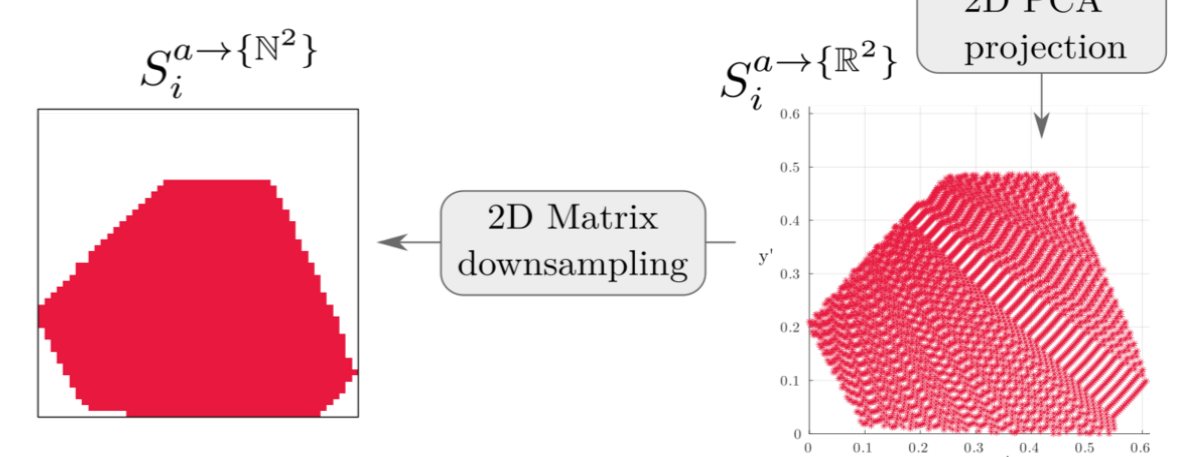
## Generalized Global Regularity Metric (G-GR)

- Extension of robust Global Regularity using 2D convex hull [4]:



For each superpixel shape  $S_i$ :

1. Spherical projection on  $\mathbb{R}^3$
2. 2D PCA projection on  $\mathbb{R}^2$
3. Downsampling for dense discretization on  $\mathbb{N}^2$
4. Measure of Global Regularity [4]



## Results

### • Validation

- Dataset. Panorama Segmentation : 75 images (1024x512) + ground truth seg. [5]
- Metrics. Contour detection (F-measure), object segmentation (ASA [6]) and G-GR

- Comparison to state-of-the-art methods:

→ Best accurate and spherically regular results with SphSPS

