



# Localization and Transformation Reconstruction of Image Regions: An Extended Congruent **Triangles Approach**

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### Motivation

Most of the existing methods to localize (sub) image relations - a subclass of near-duplicate retrieval techniques - rely on the distinctiveness of matched features of the images being compared. These sets of matching features usually include a proportion of outliers, i.e. features linking non matching regions. In approaches that are designed for retrieval purposes only, these false matches usually have a minor impact on the final ranking. However, if also a localization of regions and corresponding image transformations should be computed, these false matches often have a more significant impact. We present a novel outlier filtering approach "ECOTA" to classify outliers and describe the correlation between image regions without any prior knowledge about the content of images. The comparison with the state of the art approaches indicates that our approach is more robust than those approaches and is able to detect correlation even when most matches are outliers. Moreover, ECOTA reduces significantly the preprocessing time to filter the matches.

## **Evaluation & Results**

The performance of ECOTA is evaluated using the following settings:

- Five Datasets are used that contain images of different structures i.e. panoramas, paintings or aerial images (PANO, XOB, Aerial, PAIN, ATRANS)
- Query images are transformed images that are downscaled, rotated, flipped, shifted or cropped from the datasets
- Three kinds of keypoints are utilized: SIFT, SURF and BRISK

Time Complexity Employing various Keypoints											
Method	RANSAC	PROSAC	LMEDS	ECOTA							
SIFT	158 ms	0.72  ms	9.61mc	0.61  ms							





Comparison of RANSAC, PROSAC, LMEDS & ECOTA											
Scale	Method	Detected Correlation			Localization Error						
		RANSAC	PROSAC	LMEDS	ECOTA	RANSAC	PROSAC	LMEDS	ECOTA		
100%	SIFT	83.74	83.71	81.91	99.92	0.0016	0.0016	0.0016	0.0013		
	SURF	96.75	95.52	96.67	98.20	0.0024	0.0020	0.0020	0.0018		
	BRISK	85.37	81.65	85.60	93.16	0.0028	0.0029	0.0028	0.0025		
30%	SIFT	78.86	65.98	76.14	97.10	0.0033	0.0036	0.0031	0.0024		
	SURF	81.30	72.28	82.46	87.02	0.0040	0.0046	0.0038	0.0035		
	BRISK	69.75	59.30	67.44	75.58	0.0049	0.0057	0.0049	0.0045		
200%	SIFT	84.55	83.53	80.96	99.96	0.0016	0.0016	0.0016	0.0013		
	SURF	81.30	96.83	97.38	98.38	0.0020	0.0019	0.0019	0.0018		
	BRISK	95.94	90.18	91.72	96.51	0.0027	0.0025	0.0024	0.0021		

## **Discussion of Outliers Filtering**

RANSAC, PROSAC, LMEDS fail in correlation detection, since there are too many outliers or too few feature matches

Proposed Approach: Extended Congruent Triangles Approach



Sub-image

### **Correlation Estimation**

In the optimal case, the matched features between two near-duplicate images have a specific pattern. However, in practice, sets of false matches may appear and also construct other "false" pattern. To detect the correct pattern, we follow the steps:

For feature matches  $P_i, P_j, P_k$  and  $P'_i, P'_k$  of images I and I', check whether the corresponding triangles are congruent i.e. they fulfil the following relations:

$$\frac{l_{i}}{\max\{l_{i}, l_{j}, l_{k}\}} - \frac{l_{i}^{\prime}}{\max\{l_{i}^{\prime}, l_{j}^{\prime}, l_{k}^{\prime}\}} < \varepsilon$$
(1)





ECOTA detects 50% of features matching as outliers (red lines)



ECOTA detects the correlation even only four matches are correct (green lines)

For all of  $l_i, l_j, l_k$  and  $l_i, l_j, l_k$ , were  $L = \{l_1, l_2, ..., l_m\}$ ,  $L = \{l_1, l_2, ..., l_m\}$  are the edges of triangles

If condition 1 is justified then compute and check the relation of gradient s:

$$\varphi_{ij} = \tan 2(m_{ij}) = \tan 2\left(\frac{y_j - y_i}{x_j - x_i}\right) \quad \varphi_{ij}^{'} = \tan 2(m_{ij}^{'}) = \tan 2\left(\frac{y_j^{'} - y_i^{'}}{x_j^{'} - x_i^{'}}\right)$$

$$\left|\varphi_{ij} - \varphi_{ij}^{'}\right| < \vartheta \qquad (2)$$

- If the keypoints  $P_i, P_j, P_k$  and  $P'_i, P'_k$  relations 1 and 2 then they are correct matches.
- If relations 1 and 2 are not fulfilled for all three keypoints then the false keypoint matches is immediately determined through the gradient.

# Qualitative Discussion of Localization & Categorization

Localization of sub-images in whole scene using RANSAC (red), PROSAC (yellow), LMEDS (white) & ECOTA (blue). The ground-truth is the Green box.





### **Rotation & Flipping Estimation with ECOTA**

- To estimate the rotation instead of condition 2 we check the following condition:
  - $\left|\varphi_{ij} \varphi_{ij}\right| < \theta \pm \vartheta$ (3)
- To detect the flipping, we check the condition:

$$\left|\varphi_{ij} - \varphi_{ij}\right| = 0 \pm \vartheta \quad or \quad \left|\varphi_{ij} - \varphi_{ij}\right| = \pi \pm \vartheta$$
 (4)

We apply 1, 2, 3 and 4, on a set of best feature matches, if they satisfy the same correlation, we employ them to detect the outliers and determine the exact correlation between images without any knowledge about their contents

Correct localization only by ECOTA

# Summary

- ECOTA applies the property of congruency triangles with gradient to classify features matching into correlating group (inliers) and non-correlating (outliers).
- ECOTA uses the correlating group of matched features to:
  - Exclude the outliers of feature matches
  - Define the non-relevant images in the list of retrieved images
  - Describe the correlation between two images without any previous details about their content
  - Determine the location of one image in the other
- ECOTA reduces the computational time of correlation detection
- ECOTA outperforms RANSAC, PROSAC, LMEDS and COTA models in estimating and categorization image correlations