# Matching of Matching-Graphs - A Novel Approach for Graph Classification

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#### Introduction

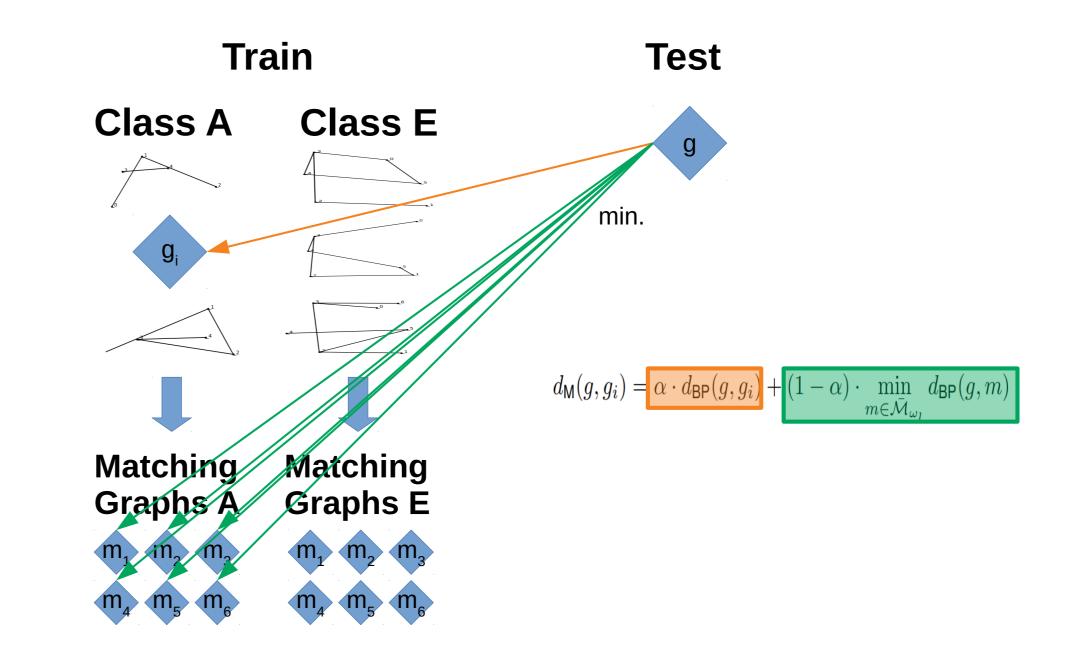
Graphs are recognized as versatile alternative to feature vectors. That is, graphs are used in diverse applications (protein function/structure prediction, signature verification or detection of Alzheimer's Disease). A large amount of graph based methods for pattern recognition have been proposed. *Graph edit distance* (GED) is one of the most flexible distance models available. GED generally offers more information than merely a dissimilarity score, namely the information of the objects actually match with each other (known as edit path).

### **Classification using matching-graphs**

The novel matching-graphs are employed in a distance based classification scenario. We define a distance measure that combines two distances with each other. A Visual illustration

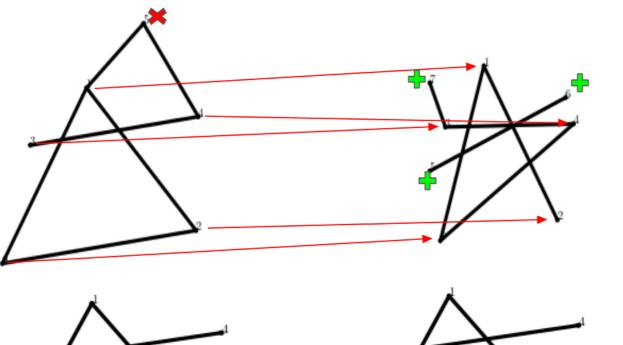
## Matching-Graphs

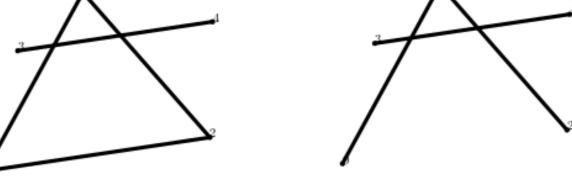
Given two graphs  $g_1$  and  $g_2$ , the basic idea of GED is to transform  $g_1$  into  $g_2$  using some *edit operations* (e.g. *insertions*, *deletions*, and *substitutions* of both nodes and edges). The set of operations used to transform  $g_1$  into  $g_2$  is called *edit path*. For each edit path, two matching-graphs  $m_{g_i \times g_j}$  and  $m_{g_j \times g_i}$ can eventually be built (for the source and the target graph  $g_i$  and  $g_j$ , respectively). To this end, all nodes that are substituted are added to the matching-graphs. All nodes that are deleted or inserted are neither considered in the two matching-graphs. Nodes without adjacent nodes are removed from the resulting matching-graphs. of this process can be seen in Fig. 2. The orange part  $d_{BP}(g,g_i)$  is the distance information between a given test graph g and a training graph  $g_i$ , calculated using the BP approximation algorithm for GED. The green part  $\min_{m \in \mathcal{M}_{\omega_l}} d_{BP}(g,m)$  is the minimum of all distances from g to all matching graphs m that are of the same class as  $g_i$ . We use  $\alpha \in [0, 1]$  as a weighting parameter.



In Fig. 1 we can see an example of the source matching-graph created from the example edit path  $\lambda = \{0 \rightarrow 0, 1 \rightarrow 1, 2 \rightarrow 0, 1 \rightarrow 1, 2 \rightarrow 0, 1 \rightarrow 1, 2 \rightarrow 0\}$ 

 $2, 3 \to 3, 4 \to 4, 5 \to \varepsilon, \varepsilon \to 5, \varepsilon \to 6, \varepsilon \to 7 \}.$ 





 $m_{g_i \times g_j}$  (unpruned)

 $m_{g_i \times g_j}$  (pruned)

Figure 1: Visualization of an edit path and the resulting matching-graphs.

Figure 2: Example of the distance calculation using matching-graphs

#### Results

The reference system, denoted as  $d_{BP}$ , is based on the GED approximation algorithm BP in conjunction with the training graphs only. Our system, denoted as  $d_M$ , uses the same GED approximation yet makes use of the novel matching-graphs.

	$k$ -NN( $d_{BP}$ )	$k\text{-}NN(d_M)$	
Data Set		Unpruned	Pruned
Letter	90.5	91.3	<b>93.1</b> o
AIDS	99.0	<b>99.7</b> °	<b>99.7</b> °
Mutagenicity	70.6	70.0	70.5

Table 1: Results Table. On the left the baseline and on the right our approach. The  $\circ$  indicates a statistically significant improvement over the reference system using a Z-Test at significance level  $\alpha = 0.05$ 

We observe that the distance-based classification achieves

To handle the edges, we propose two different approaches: pruned and unpruned matching-graphs. For a pruned matching-graph if two nodes  $u_1, u_2 \in V_i$  of a source graph  $g_i$  are substituted with nodes  $v_1, v_2 \in V_j$  in a target graph  $g_j$  and there is an edge  $(u_1, u_2) \in E_i$  available,  $(u_1, u_2)$  is actually included in the matching-graph  $m_{g_i \times g_j}$  if, and only if, there is an edge  $(v_1, v_2)$  available in  $E_j$ . In an unpruned matching-graph it is included regardless whether or not edge  $(v_1, v_2)$  is available in  $E_j$ . better results with  $d_M$  rather than  $d_{BP}$  on two data sets (Letter and AIDS) and with both strategies (pruned and unpruned edges). On the Mutagenicity data set a slight - non statistically significant - deterioration is observed with our novel approach.

Hence, we conclude that the integration of matching-graphs can lead to a more accurate determination of a dissimilarity score using GED.