









Trainable Spectrally Initializable Matrix Transformations in CNNs

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Key Contributions

Proof-of-concept and implementation for a novel architectural component, which leverages trainable linear matrix transformation module

→ can perform global transformation

PyTorch based open-source implementations as a pip installable python package¹ and integrated into the DeepDIVA² deep learning framework

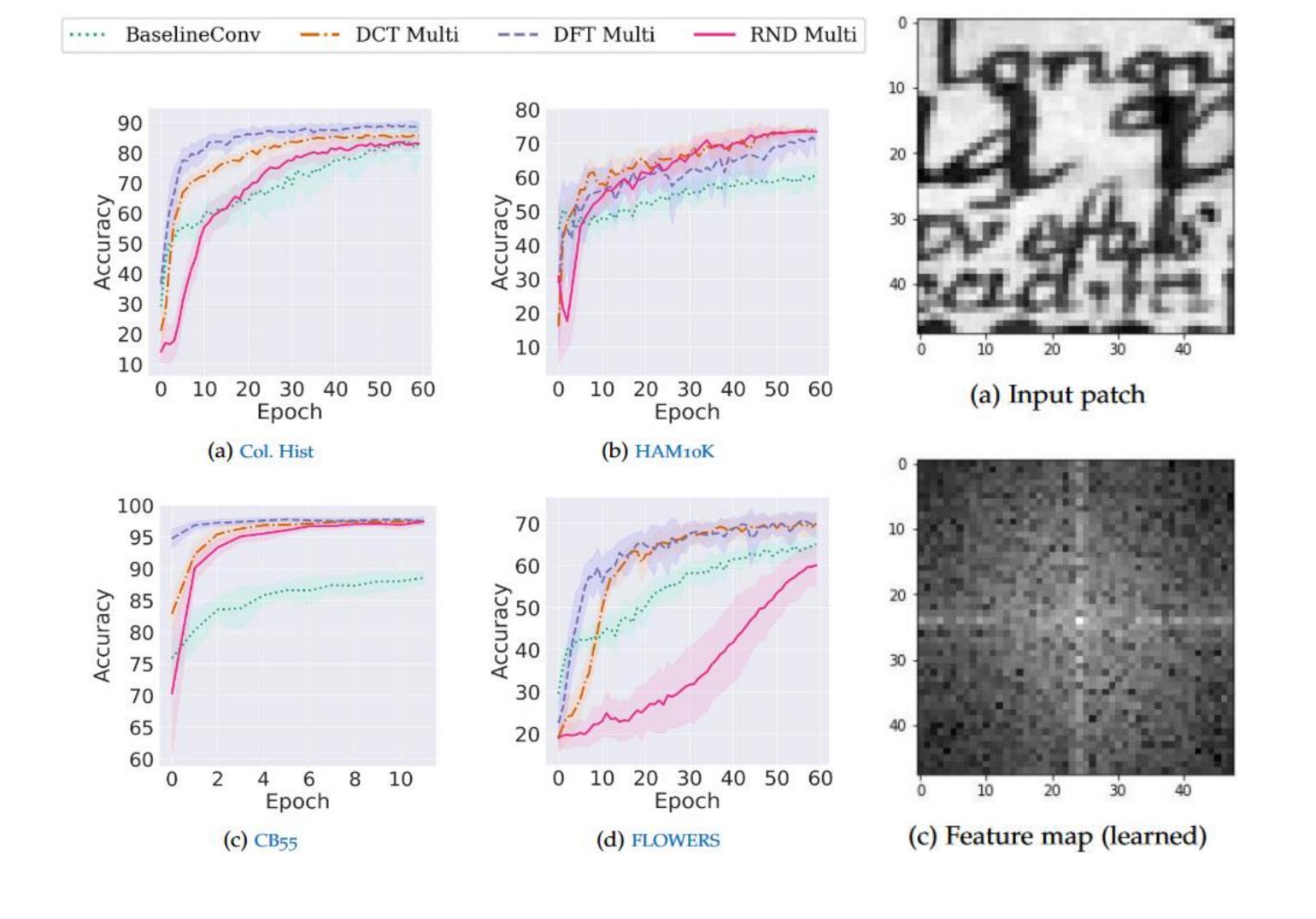
→ enabling full reproducibility of experiments

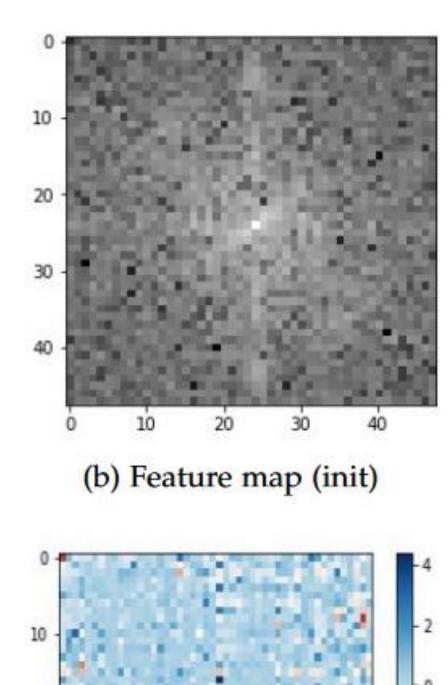
Why Should One Care?

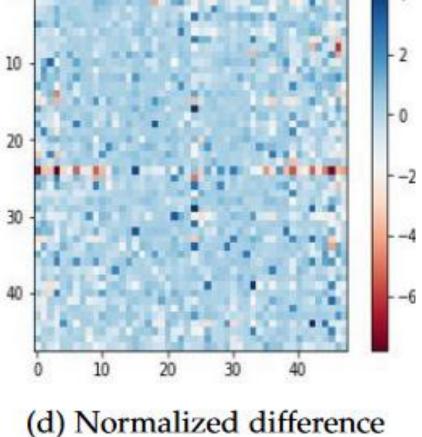
Vanilla CNN struggle at applying global transformations (e.g., translation, rotation, scaling, ...) and are biased towards texture for object recognition.

Global transformations are useful for texture analysis

Experimental Analysis







Proposed Module

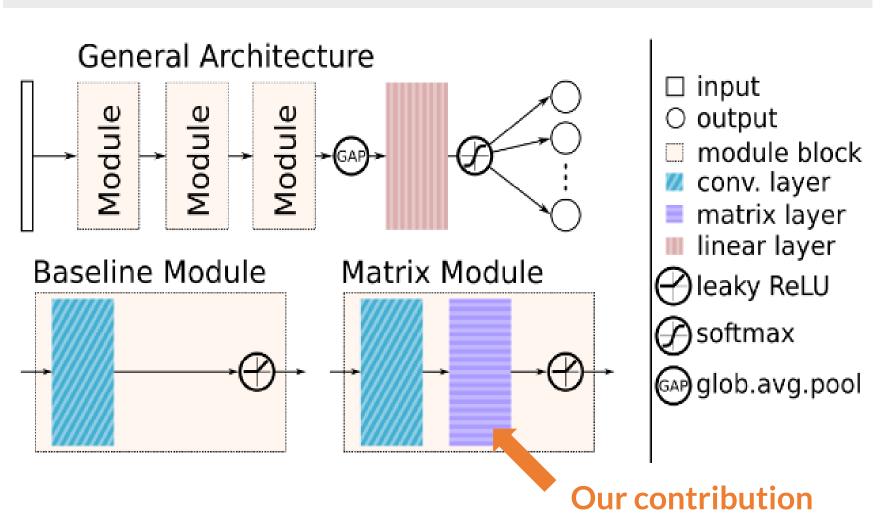
Matrix transform layer:

$$y_{mt} = W_1 \cdot x \cdot W_2^T$$

Instead of traditional:

$$y_{nn} = W \cdot x + b$$

Network Design



Results Overview

Models with matrix transformations outperform the baseline

Matrix transforms are beneficial for convergence

The DFT variants appears to be the best performing

Further research should also focus tasks such as video or medical tomography data analysis

Conclusion

Our component overcomes traditional CNN limitation and enables applying global transformations

Empirical results shows this is beneficial in terms of learning speed and final performances on a image classification task

Spectral initialization as DCT or DFT brings substantial speedups in terms of convergence, when compared to random initialization

- 1. Novel Module https://github.com/NarayanSchuetz/SpectralLayersPyTorch
- 2. Deep Learning Framework https://github.com/NarayanSchuetz/DeepDIVA