

# Adaptive Context-Aware Discriminative Correlation Filters for Robust Visual Object Tracking

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# Task Definition

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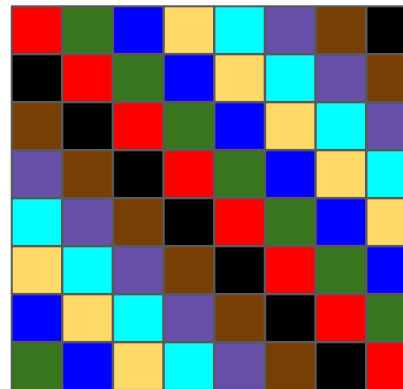
automatically track a target in a video sequence by predicting its location and scale

# Background - Discriminative Correlation Filters



$x$

original vector

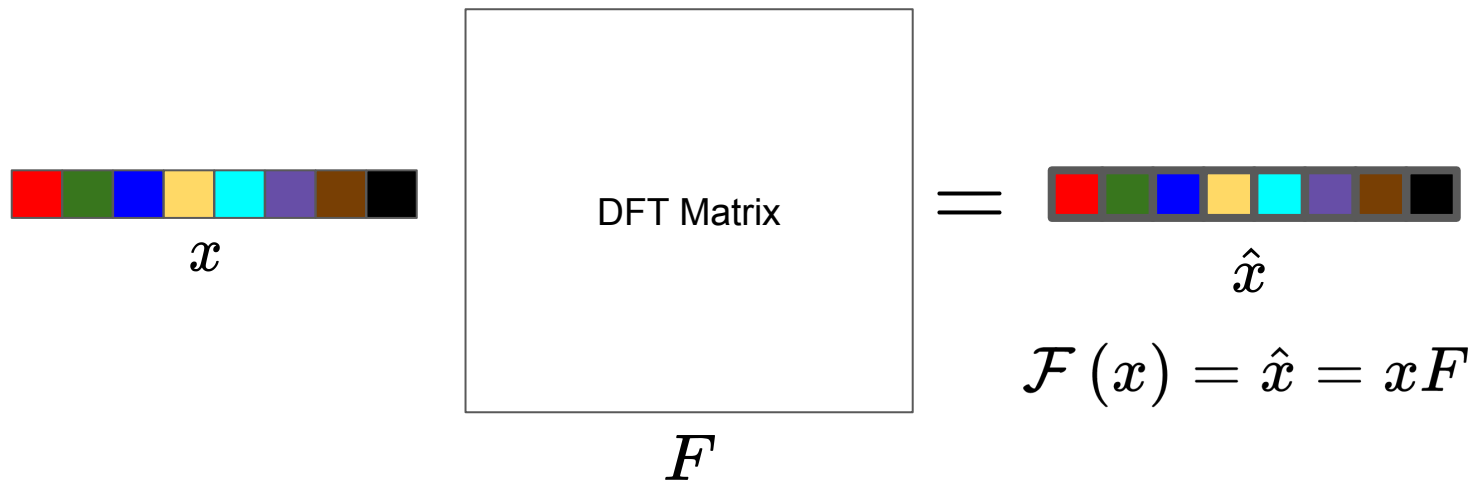


$X$

circulant matrix

Gray, Robert M. "Toeplitz and circulant matrices: A review." *Foundations and Trends® in Communications and Information Theory* 2.3 (2006): 155-239.

# Background - Discriminative Correlation Filters



Stockham Jr, Thomas G. "High-speed convolution and correlation." *Proceedings of the April 26-28, 1966, Spring joint computer conference.* ACM, 1966.

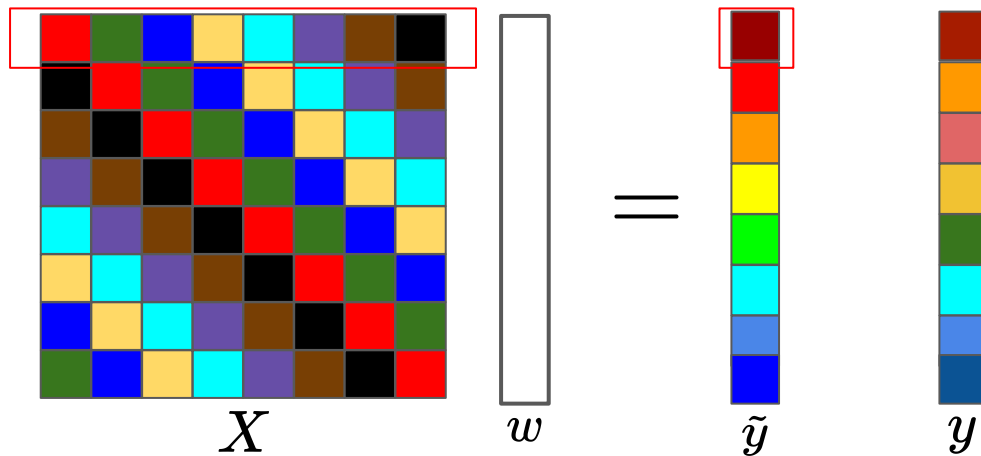
# Background - Discriminative Correlation Filters

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$$\text{diag}(\hat{x}) = \text{diag}(xF) = F^H XF \quad X = F \text{diag}(\hat{x}) F^H$$

$$\boxed{X^H X} = F \text{diag}(\hat{x}^* \odot \hat{x}) F^H$$

# Background - Discriminative Correlation Filters



The diagram illustrates the discriminative correlation filter equation. It shows a matrix  $X$  (8x8) being multiplied by a filter vector  $w$  (8x1) to produce a vector  $\tilde{y}$  (8x1). This vector  $\tilde{y}$  is then compared to a target vector  $y$  (8x1) to find the minimum L2 norm difference, regularized by the L2 norm of  $w$ .

$$\min \|Xw - y\|_2^2 + \lambda \|w\|_2^2$$

# Background - Discriminative Correlation Filters

$$\min \|Xw - y\|_2^2 + \lambda \|w\|_2^2$$

$$w = (X^T X + \lambda I)^{-1} X^T y \longleftarrow$$

$$\begin{aligned} X^H X &= F \text{diag} (\hat{x}^* \odot \hat{x}) F^H \\ X &= F \text{diag} (\hat{x}) F^H \end{aligned}$$

$$\hat{w} = \frac{\hat{x}^* \odot \hat{y}}{\hat{x}^* \odot \hat{x} + \lambda}$$

**the original domain**  
 matrix multiplication  
 inverse matrix

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**the frequency domain**  
 element-wise multiplication  
 element-wise division

Henriques, João F., et al. "High-speed tracking with kernelized correlation filters." *IEEE transactions on pattern analysis and machine intelligence* 37.3 (2015): 583-596.

# Background - Discriminative Correlation Filters

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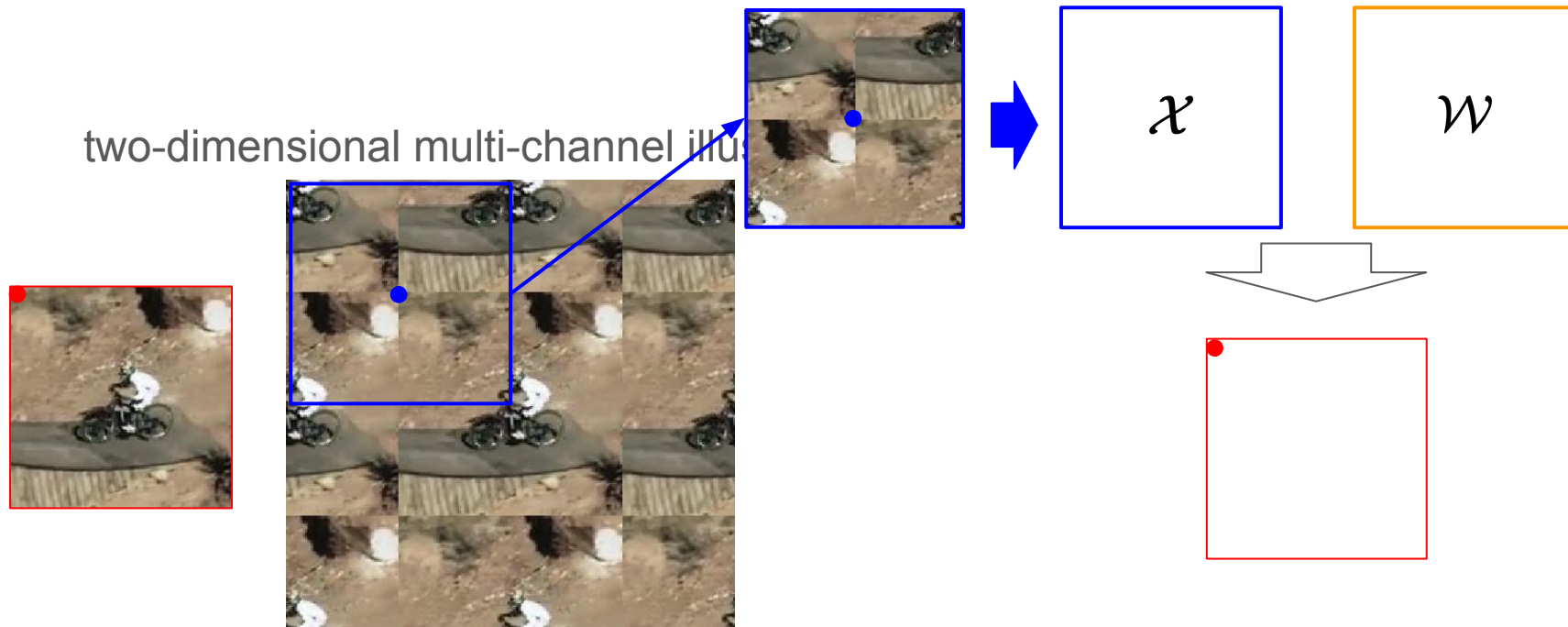
Advantages:

1. data augmentation
2. superior efficiency

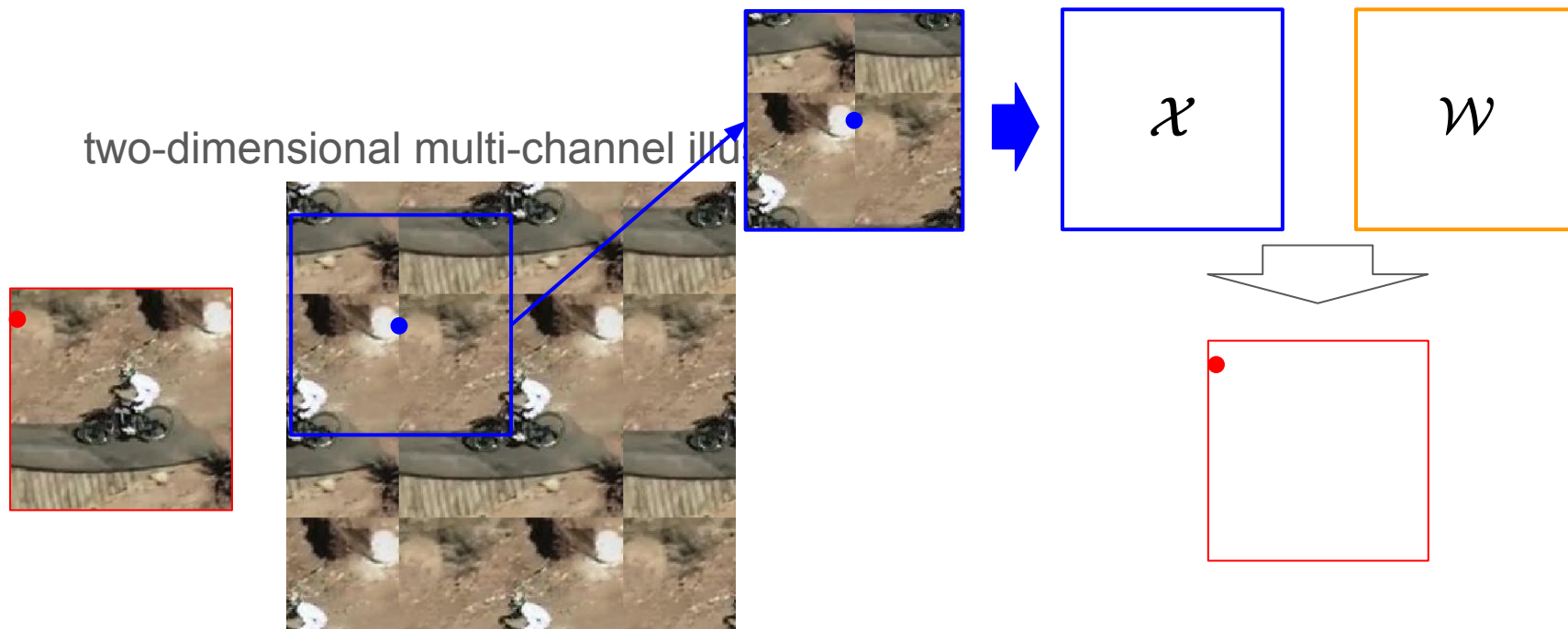
$$\begin{aligned} 1 &\rightarrow n \\ \mathcal{O}(n^3) &\rightarrow \mathcal{O}(n \log n) \end{aligned}$$



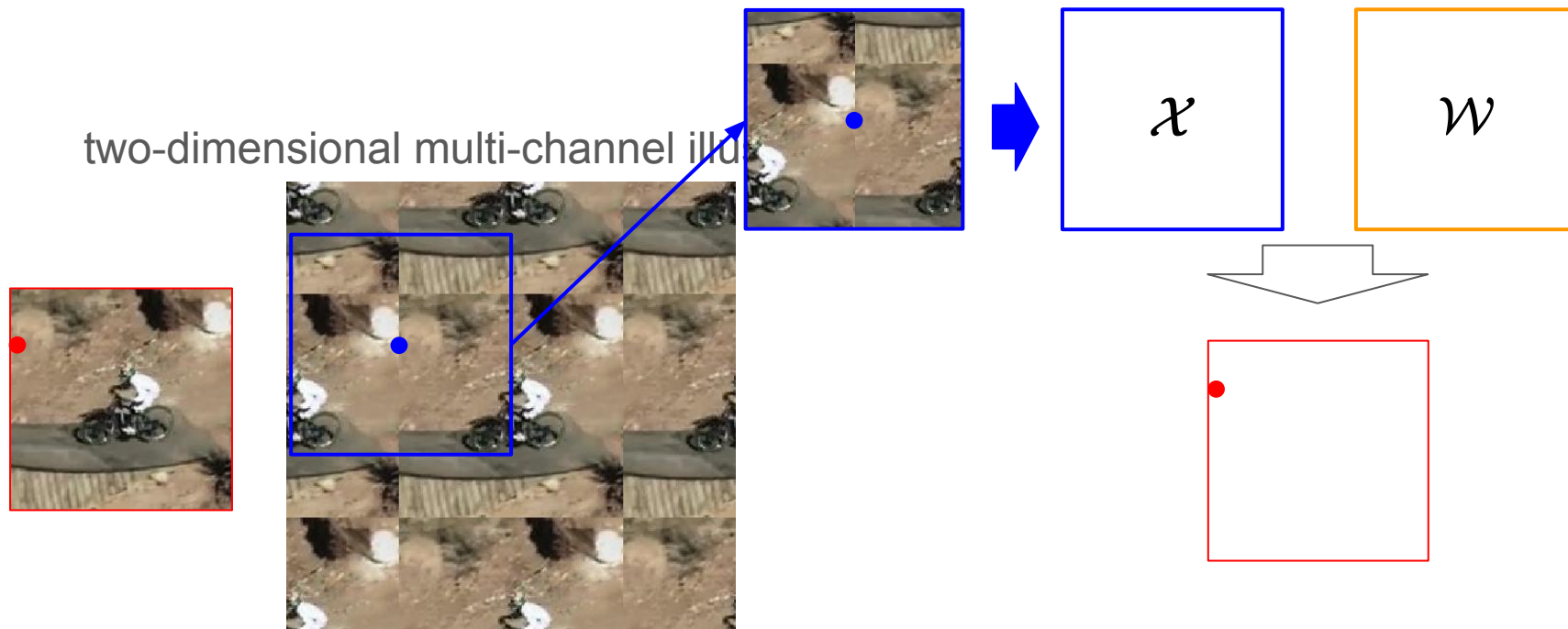
# Background - Discriminative Correlation Filters



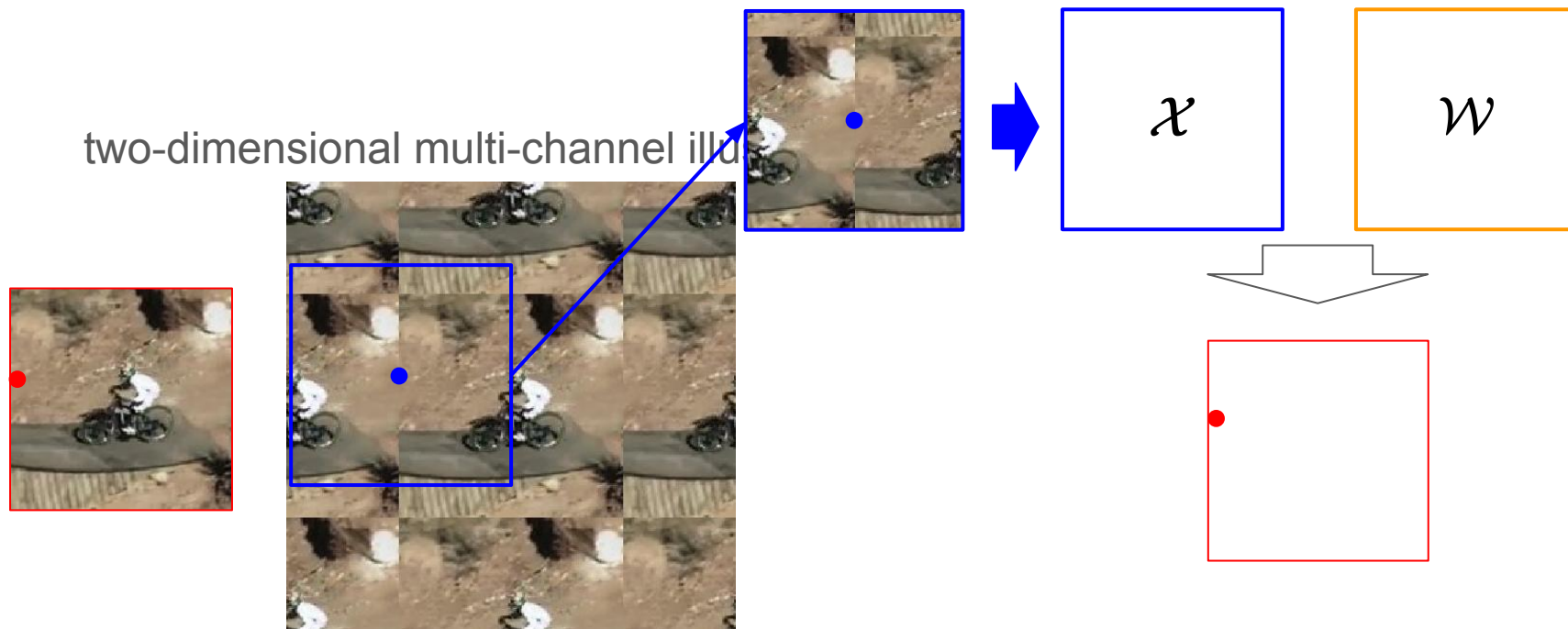
# Background - Discriminative Correlation Filters



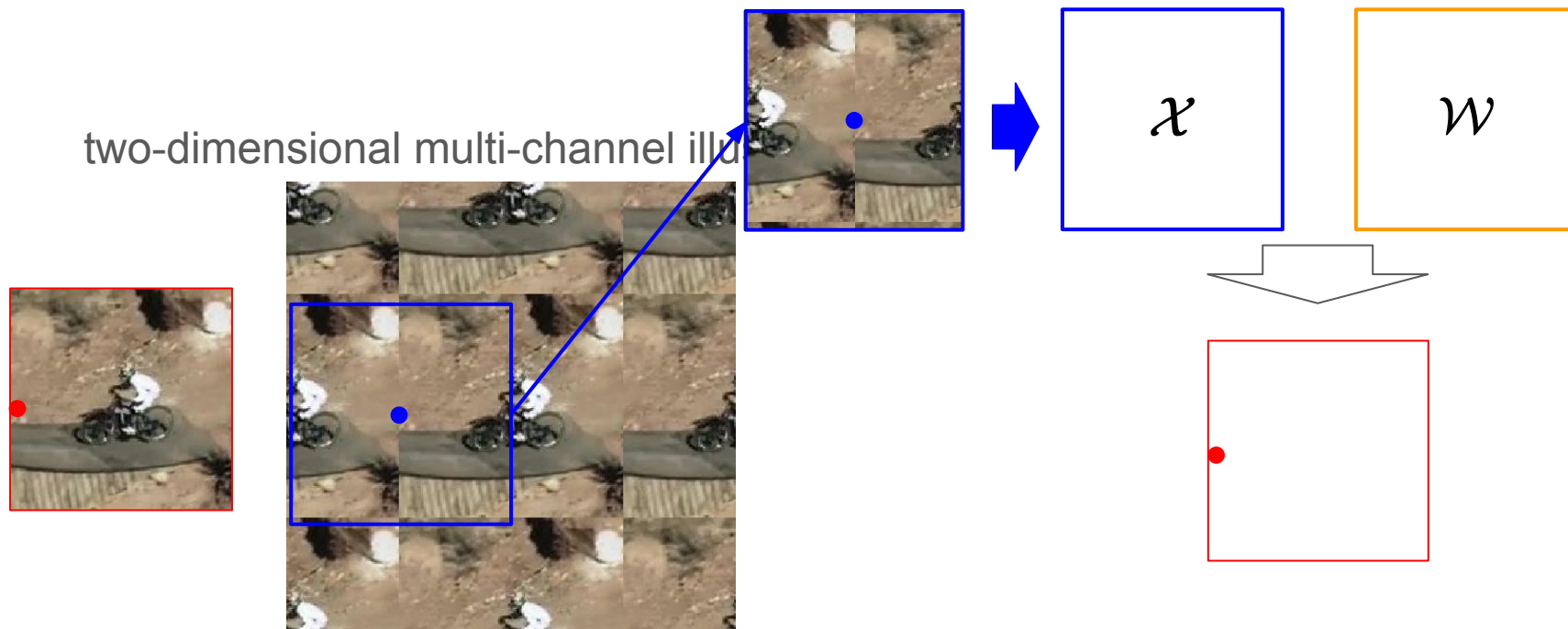
# Background - Discriminative Correlation Filters



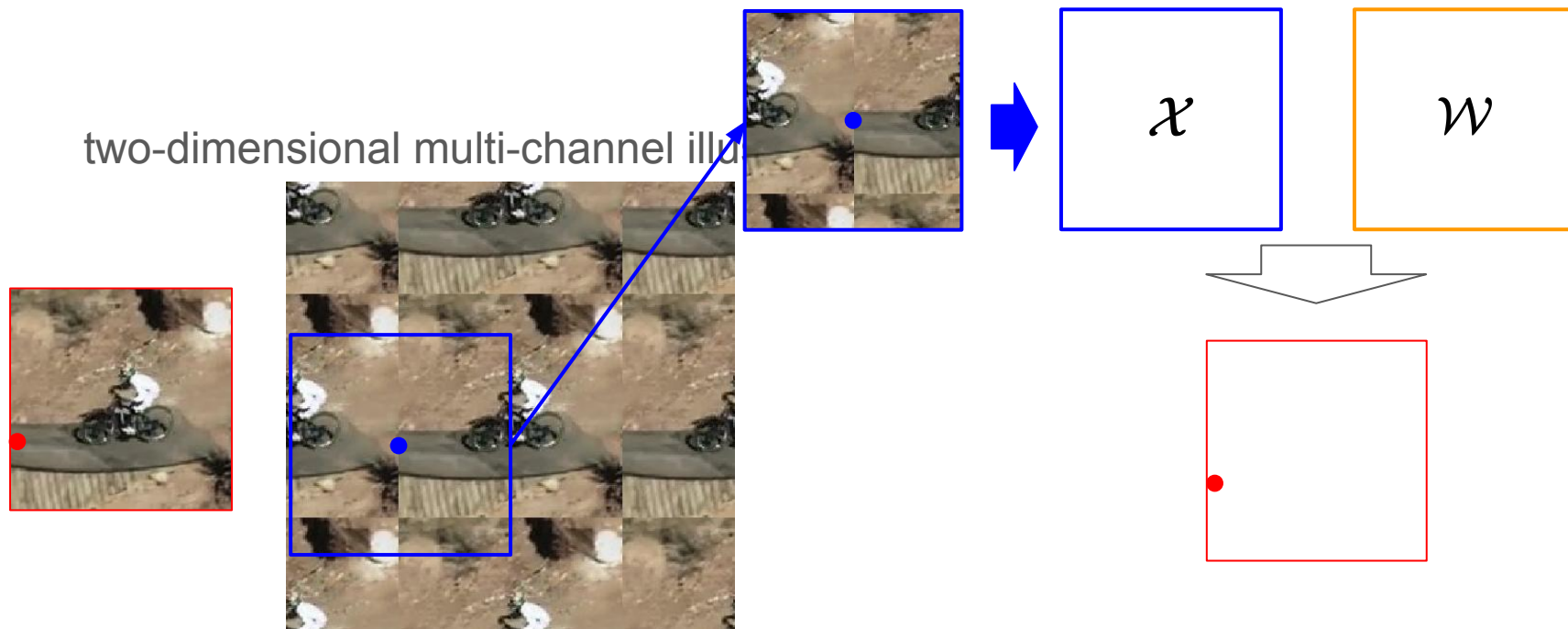
# Background - Discriminative Correlation Filters



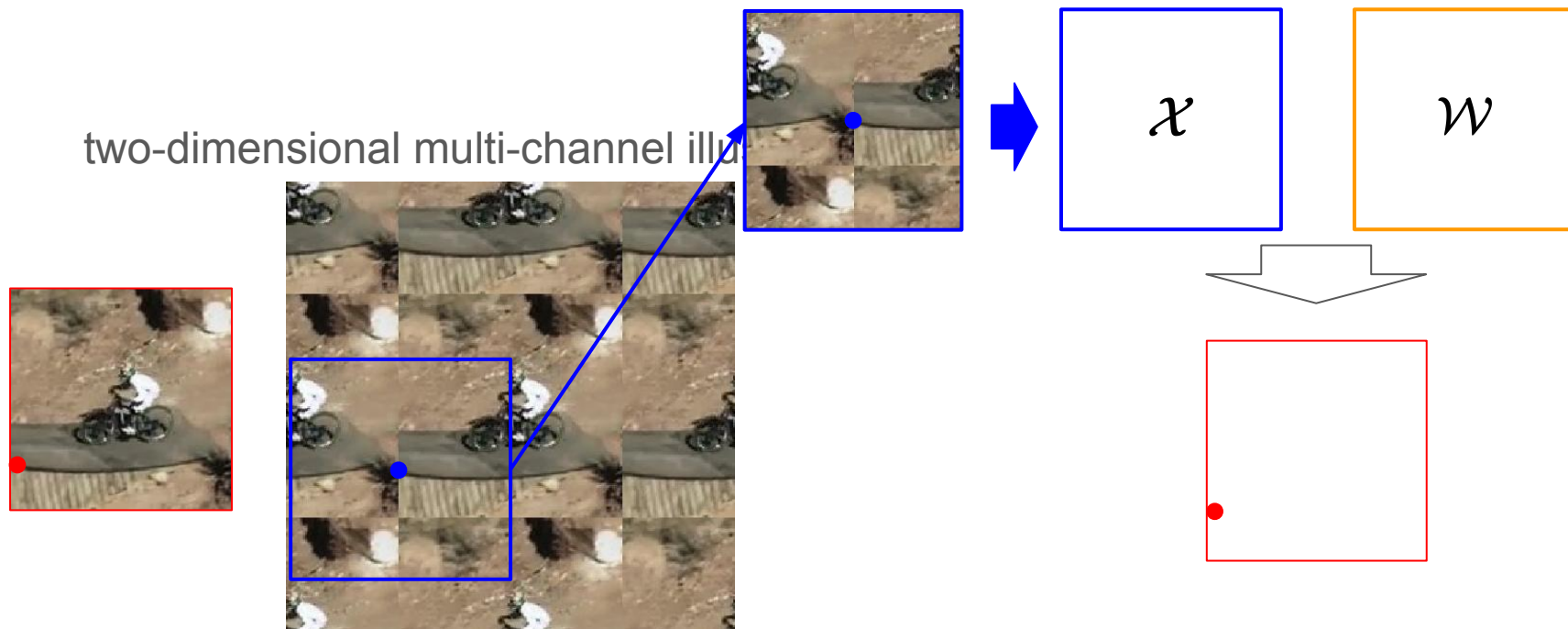
# Background - Discriminative Correlation Filters



# Background - Discriminative Correlation Filters

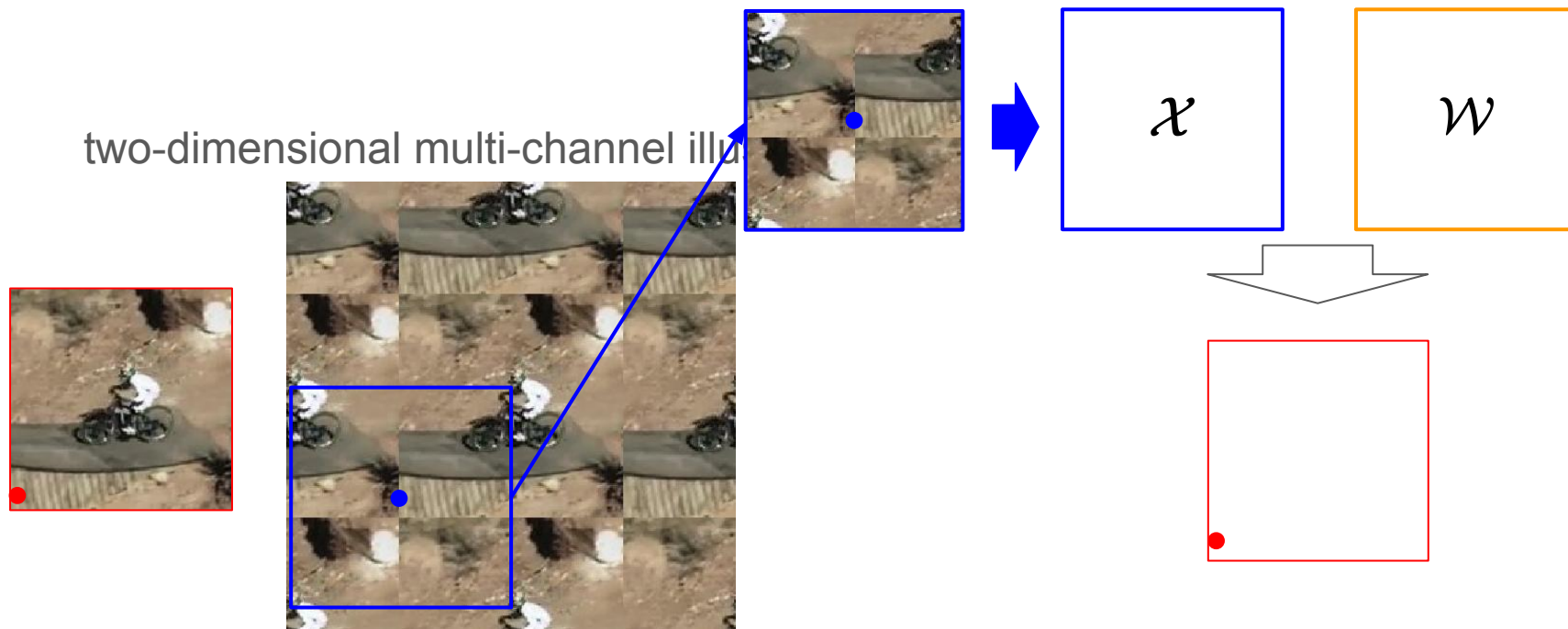


# Background - Discriminative Correlation Filters



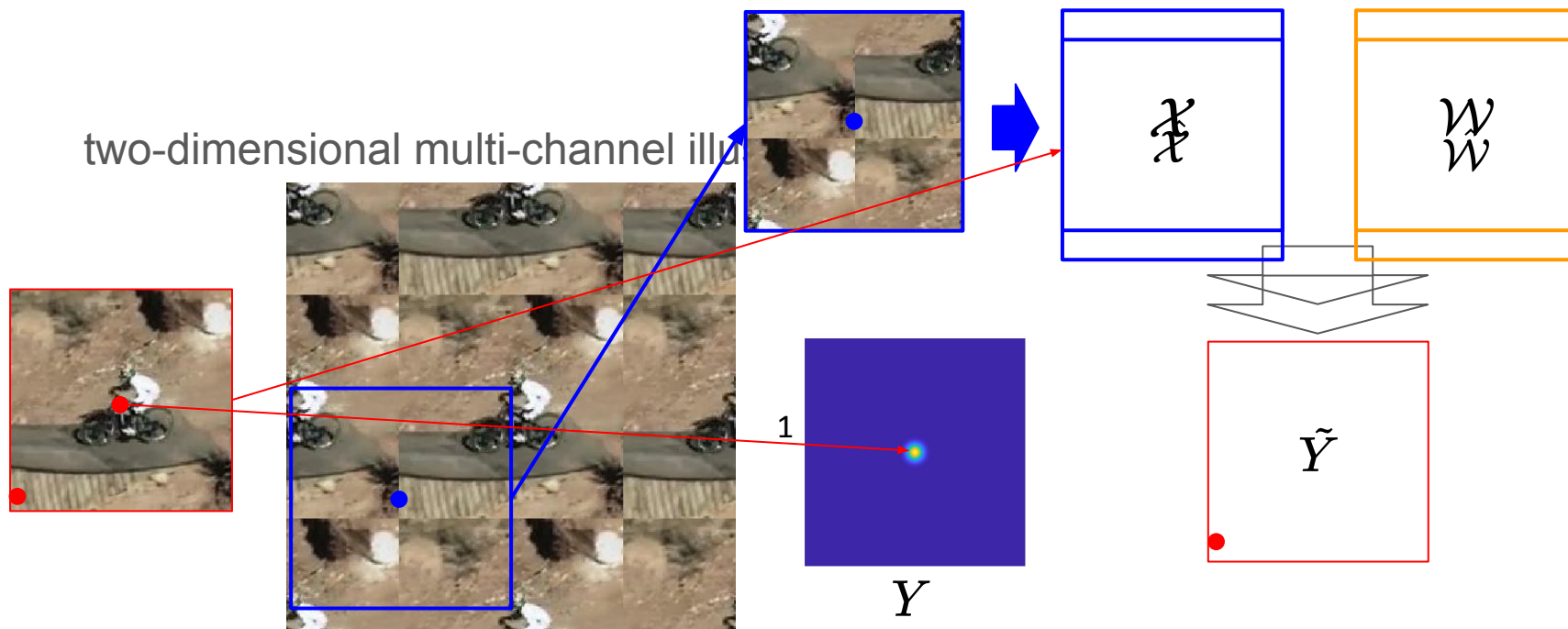


# Background - Discriminative Correlation Filters





# Background - Discriminative Correlation Filters

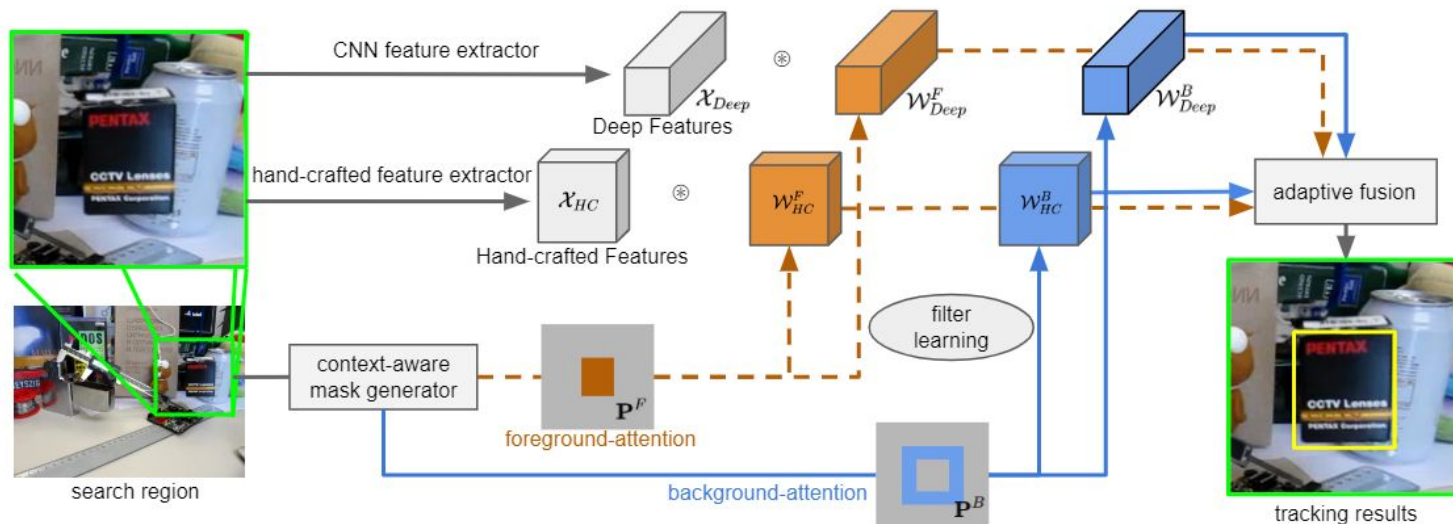


# ACA-DCF - Motivation

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Explore the foreground / background context-aware clues within the hand-crafted and deep feature representations to enhance discrimination and robustness.

# ACA-DCF - Framework



*The proposed adaptive context-aware DCF method using both hand-crafted and deep features. The proposed context-aware mask generator is instrumental in applying foreground-background attention to the learned filters. The corresponding responses are adaptively fused to generate the final result.*

# ACA-DCF - Context-aware masks

We design our context-aware attention masks with two complementary components, the foreground-attention mask  $\mathbf{P}^F$  as:

$$p_{ij}^F = \begin{cases} 1 \times 10^{-3} & (i, j) \in \mathcal{F} \\ 1 & (i, j) \notin \mathcal{F} \end{cases}$$

and the background-attention mask  $\mathbf{P}^B$  as:

$$p_{ij}^B = \begin{cases} 1 \times 10^{-3} & (i, j) \in \mathcal{B} \\ 1 & (i, j) \notin \mathcal{B} \end{cases}$$

where  $p_{ij}$  is the  $i$ -th row  $j$ -th column element of  $\mathbf{P}$ .  $\mathcal{F}$  and  $\mathcal{B}$  are the target region and surrounding region.

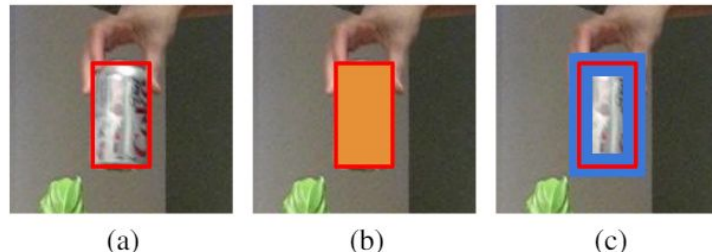


Illustration of the proposed complementary attention mechanism based context-aware mask generator: (a) target bounding box; (b) foreground-attention mask; and (c) background-attention mask.

# ACA-DCF - Formulation

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To better illustrate the spatial information, we formulate our ACA-DCF in a 2D and multi-channel manner:

$$\min \left\| \sum_{k=1}^C \mathbf{X}^k * \mathbf{W}^k - \mathbf{Y} \right\|_F^2 + \lambda \sum_{k=1}^C \left\| \mathbf{P} \odot \mathbf{W}^k \right\|_F^2,$$

where  $\mathbf{X}^k \in \mathbb{R}^{N \times N}$  is the  $k$ -th channel representation of a 3-rd order feature tensor  $\mathcal{X} \in \mathbb{R}^{N \times N \times C}$ ,  $\mathbf{W}^k \in \mathbb{R}^{N \times N}$  is the  $k$ -th corresponding filter that is a slice of the filter tensor  $\mathcal{W} \in \mathbb{R}^{N \times N \times C}$ , and  $\mathbf{P}^{N \times N}$  is the designed spatial regularisation mask.

# ACA-DCF - Optimization

We use the augmented Lagrange method to optimise the objective function.

We use slack variable  $\mathcal{W}' = \mathcal{W}$  (for each  $k$ ,  $\mathbf{W}'^k = \mathbf{W}^k$ ) and construct the following Lagrange function:

$$\begin{aligned} \mathcal{L} = & \left\| \sum_{k=1}^C \mathbf{X}^k * \mathbf{W}^k - \mathbf{Y} \right\|_F^2 + \lambda \sum_{k=1}^C \left\| \mathbf{P} \odot \mathbf{W}'^k \right\|_F^2 \\ & + \frac{\mu}{2} \sum_{k=1}^C \left\| \mathbf{W}^k - \mathbf{W}'^k + \frac{\mathbf{\Gamma}^k}{\mu} \right\|_F^2, \\ & \begin{cases} \hat{\mathbf{w}}_{i,j} = \left( \mathbf{I} - \frac{\hat{\mathbf{x}}_{i,j} \hat{\mathbf{x}}_{i,j}^\top}{\mu/2 + \hat{\mathbf{x}}_{i,j} \hat{\mathbf{x}}_{i,j}^\top} \right) \mathbf{g} \\ \mathbf{W}'^k = (\mathbf{I} - \mathbf{P}) \odot \frac{\mu \mathbf{W}^k + \mathbf{\Gamma}^k}{2\lambda + \mu} \\ \mathbf{\Gamma} = \mathbf{\Gamma} + \mu (\mathcal{W} - \mathcal{W}') \end{cases} \\ & \mathbf{g} = \left( \hat{\mathbf{x}}_{i,j} \hat{\mathbf{y}}_{i,j} + \mu \hat{\mathbf{w}}_{i,j}' - \mu \hat{\gamma}_{i,j} \right) / \mu \end{aligned}$$

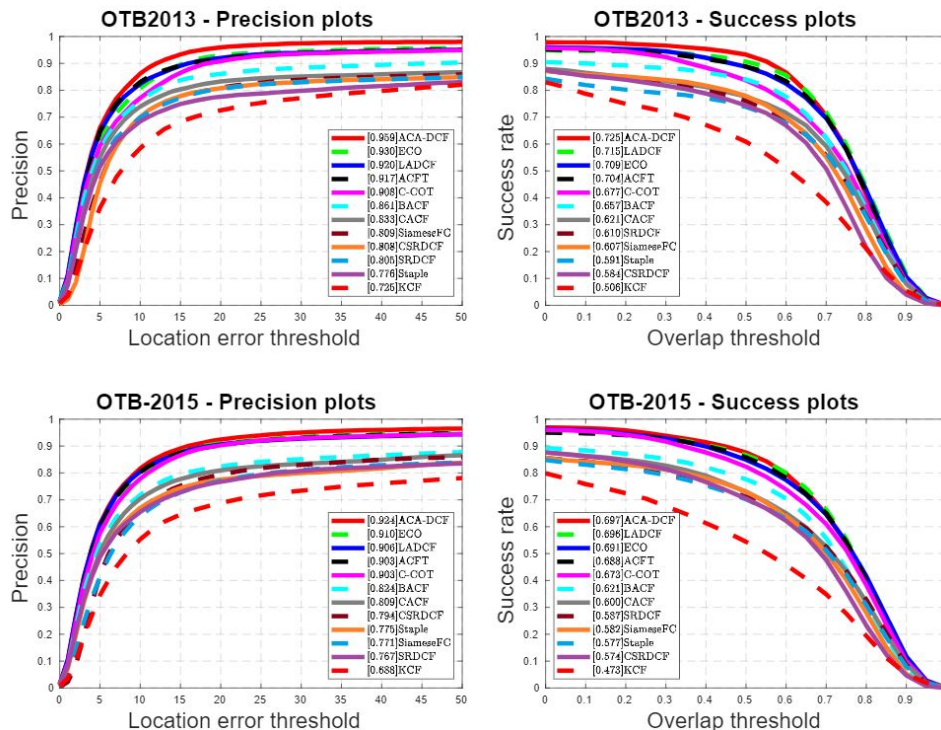
# ACA-DCF - Optimization

Solution:

$$\begin{cases} \hat{\mathbf{w}}_{i,j} = \left( \mathbf{I} - \frac{\hat{\mathbf{x}}_{i,j} \hat{\mathbf{x}}_{i,j}^\top}{\mu/2 + \hat{\mathbf{x}}_{i,j}^\top \hat{\mathbf{x}}_{i,j}} \right) \mathbf{g} \\ \mathbf{W}'^k = (\mathbf{1} - \mathbf{P}) \odot \frac{\mu \mathbf{W}^k + \mathbf{\Gamma}^k}{2\lambda + \mu} \\ \mathbf{\Gamma} = \mathbf{\Gamma} + \mu (\mathcal{W} - \mathcal{W}') \end{cases}$$

$$\mathbf{g} = \left( \hat{\mathbf{x}}_{i,j} \hat{y}_{i,j} + \mu \hat{\mathbf{w}}'_{i,j} - \mu \hat{\gamma}_{i,j} \right) / \mu$$

# Experiments



*Evaluation on OTB2013 and OTB2015, using the precision plots with DP in the legend and the success plots with AUC in the legend.*



# Experiments

	STAPLE+	EBT [34]	DDC	Staple [17]	MLDF	SSAT	TCNN [35]	C-COT [21]	ACA-DCF
<b>EAO</b>	0.286	0.291	0.293	0.295	0.311	0.329	<b>0.327</b>	<b>0.331</b>	<b>0.385</b>
<b>Accuracy</b>	<b>0.559</b>	0.465	0.542	0.547	0.492	<b>0.579</b>	0.555	0.541	<b>0.581</b>
<b>Robustness</b>	0.37	0.25	0.34	0.38	<b>0.23</b>	0.29	0.27	<b>0.24</b>	<b>0.21</b>

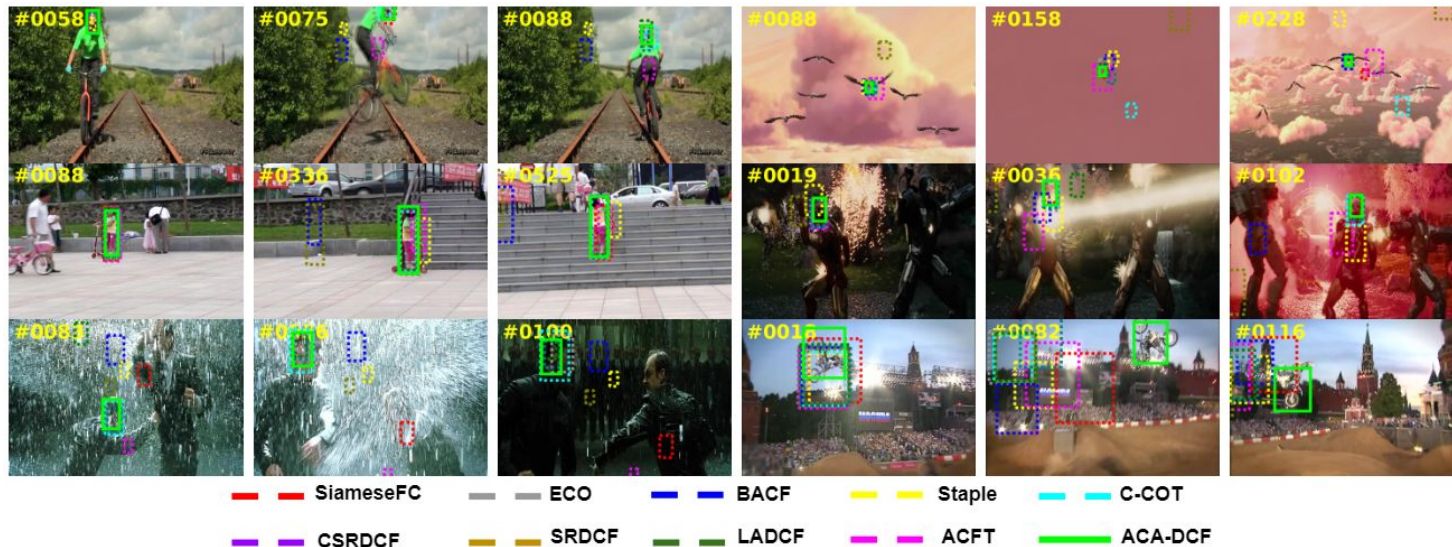
*Tracking results on VOT2016.*

# Experiments

		DEF	IPR	IV	OPR	OV	SV	LR
	DSST [36] [TPAMI-17]	56.2/40.0	70.7/47.4	73.9/49.6	65.8/43.7	48.1/36.5	64.3/39.5	67.8/30.5
	Staple [17] [CVPR-16]	72.9/54.4	75.3/54.4	76.9/58.8	72.4/52.8	66.1/48.1	72.7/52.5	69.5/39.6
	SRDCF [15] [ICCV-15]	70.7/53.1	69.6/51.7	74.5/58.9	71.3/53.4	58.2/45.8	73.1/55.4	74.2/51.0
	BACF [26] [ICCV-17]	77.8/58.2	79.5/58.4	83.0/64.2	78.7/58.4	76.5/55.2	77.4/57.6	79.5/51.4
	CFNet [24] [CVPR-17]	69.6/50.8	76.8/57.2	70.5/54.9	74.1/54.7	53.6/42.3	72.6/55.0	81.0/58.6
	CSRDCF [27] [CVPR-17]	73.5/52.4	73.6/51.9	73.2/53.9	72.1/51.5	65.1/49.6	75.0/52.8	81.3/45.1
Mean	ACFN [37] [CVPR-17]	77.2/53.5	78.0/54.3	78.8/56.7	77.7/54.3	67.3/49.7	76.0/54.8	81.8/51.5
DP/AUC (%/%)	STAPLE_CA [38] [CVPR-17]	76.0/56.6	80.6/57.4	81.6/61.3	75.8/55.2	69.7/50.9	75.3/54.1	81.9/44.8
	TRACA [39] [CVPR-18]	76.9/56.1	80.6/57.6	84.1/62.2	82.3/59.3	68.0/53.4	76.1/55.2	86.0/50.2
	CREST [25] [ICCV-17]	77.6/56.9	85.3/61.7	87.6/64.4	84.2/61.5	73.4/56.6	78.6/57.2	86.6/47.3
	SiamFC [4] [ECCV-16]	69.0/50.6	74.2/55.7	73.6/56.8	75.6/55.8	66.9/50.6	73.5/55.2	90.0/61.8
	MetaT [40] [ECCV-18]	83.8/62.0	87.7/63.5	86.4/63.4	85.2/62.7	72.3/56.0	80.3/58.2	90.1/47.2
	MC PF [41] [TPAMI-18]	81.6/57.0	88.8/62.0	88.1/62.8	86.7/61.9	76.4/55.3	86.2/60.3	96.3/58.7
	C-COT [21] [ECCV-16]	85.9/61.4	87.7/62.7	88.4/68.2	89.9/65.2	89.5/64.8	88.1/65.4	97.5/62.9
	ECO [18] [CVPR-17]	85.9/63.3	89.2/65.5	91.4/71.3	90.7/67.3	91.3/66.0	87.9/66.6	88.2/59.1
	LADCF [13] [TIP-19]	87.2/65.2	88.3/65.9	89.0/70.5	90.4/68.2	91.0/67.2	88.2/67.0	87.9/61.7
	ACA-DCF	89.3/64.8	93.1/67.8	93.3/72.6	91.8/68.0	94.0/68.0	90.3/68.1	99.6/70.7

*The DP and AUC results on OTB2015, parameterised by 7 attributes.*

# Experiments



Examples of qualitative tracking results on challenging sequences (Left column top to down: Biker, Girl2, and Matrix. Right column top to down: Bird1, Ironman, and MotorRolling). The colour bounding boxes denote the results of SiameseFC, ECO, BACF, Staple, C-COT, CSRDCF, SRDCF, LADCF, ACFT, and ACA-DCF, respectively.

# Conclusion

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We improve the DCF formulation by designing a novel adaptive context-aware mechanism.

- The information contents of a target and its surroundings are analysed by the proposed complementary foreground-background attention mechanism.
- The two sources of information are fused by a novel adaptive fusion strategy to further improve the robustness with the consideration of the dynamics of target and background appearance variations.
- The experimental results obtained on well-known benchmarking datasets demonstrate the effectiveness and robustness of our method. It was shown to achieve superior performance over the state-of-the-art visual object tracking algorithms.

Thank you