# Motion segmentation with pairwise matches and unknown number of motions 

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## Introduction

Motion segmentation: the goal is to classify points in multiple images based on the moving object they belong to.


Assumption: the number of motions is unknown.

## Introduction

Scenario: two-frame correspondences are available

unfeasible

realistic


Unknown
correspondences


Two frame correspondences

Trajectory clustering

## Contribution

In this paper we propose a segmentation approach that combines local/partial results independently obtained from pairs of images.

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We extend a recent work to the case of an unknown number of motions.
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F. Arrigoni and T. Pajdla Robust motion segmentation from pairwise matches ICCV (2019)

## Proposed Method

1. Motion segmentation is solved independently on different image pairs, by fitting an unknown number of fundamental matrices to correspondences.
$\square$ L. Magri and A. Fusiello T-Linkage: a continuous relaxation of J- Linkage for multi-model fitting CVPR (2014)
2. Such partial results are combined in order to get a multi-frame segmentation.


## Proposed Method

Idea: all the two-frame segmentations involving a fixed image provide an estimate for the segmentation of that image.


Two challenges have to be addressed:

- ambiguity - each two-frame segmentation considers its own labelling of the motions;
- noise - each two-frame segmentation may contain some errors.


## Proposed Method

Graph: each vertex corresponds to one image pair; an edge is drawn between two vertices each time the associated pairs have one image in common.


- For each edge a permutation is computed via a linear assignment problem.
H. W. Kuhn The Hungarian method for the assignment problem Naval Research Logistics Quarterly 2 (1955)
- Permutations for all the nodes are computed by permutation synchronization with unknown number of motions.
$\square$ E. Maset, F. Arrigoni, and A. Fusiello Practical and efficient multi-view matching ICCV (2017)R. Tron, X. Zhou, C. Esteves, and K. Daniilidis Fast multi-image matching via density-based clustering ICCV (2017)


## Proposed Method

For each point in a given image, several putative labels are available: the most frequent label (mode) is chosen. Outlier/missing labels are ignored.


This procedure is repeated for all the images in order to produce the output segmentation.


Image 1


Image 2


Image 3


Image 4


Image 5

## Experiments

|  |  |  | Our Method |  |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Error[\%] | Points[\%] | Error[\%] | Points[\%] |  |  |  |  |  |  |  |
| Dataset | $d$ | $n$ | $p$ | $\widehat{d}$ | Error[\%] | Points[\%] | Eyde | Synch |  |  |
| Pen | 2 | 6 | 4550 | 2 | 1.55 | 89.08 | $\mathbf{0 . 5 8}$ | 80.07 | 0.82 | 83.23 |
| Pouch | 2 | 6 | 4971 | 2 | $\mathbf{1 . 3 9}$ | 60.79 | 3.79 | 65.34 | 4.15 | 69.89 |
| Needlecraft | 2 | 6 | 6617 | 2 | 1.80 | 67.07 | $\mathbf{0 . 8 3}$ | 72.81 | 1.04 | 76.76 |
| Biscuits | 2 | 6 | 13158 | 2 | 1.12 | 90.42 | $\mathbf{0 . 4 7}$ | 84.47 | 0.51 | 87.28 |
| Cups | 2 | 10 | 14664 | 2 | 2.05 | 71.31 | $\mathbf{0 . 5 6}$ | 65.42 | 1.01 | 69.82 |
| Tea | 2 | 10 | 32612 | 2 | 0.69 | 85.21 | $\mathbf{0 . 2 9}$ | 81.70 | 28.12 | 52.21 |
| Food | 2 | 10 | 36723 | 2 | 0.78 | 82.34 | $\mathbf{0 . 3 6}$ | 76.19 | 0.56 | 80.66 |
| Penguin | 2 | 6 | 5865 | 2 | 1.36 | 66.60 | $\mathbf{0 . 7 6}$ | 69.17 | 44.21 | 46.97 |
| Flowers | 2 | 6 | 7743 | 2 | 1.51 | 75.50 | $\mathbf{1 . 2 3}$ | 73.65 | 1.62 | 77.28 |
| Pencils | 2 | 6 | 2982 | 2 | $\mathbf{3 . 0 9}$ | 51.01 | 3.80 | 65.33 | 27.53 | 40.44 |
| Bag | 2 | 7 | 6114 | 2 | 2.78 | 52.91 | $\mathbf{1 . 5 2}$ | 57.95 | 25.92 | 54.27 |
| Bears | 3 | 10 | 15888 | 3 | $\mathbf{3 . 4 8}$ | 68.21 | 4.82 | 73.65 | 38.95 | 74.59 |

[Dataset] https://github.com/federica-arrigoni/ICCV_19
[Mode] F. Arrigoni and T. Pajdla Robust motion segmentation from pairwise matches ICCV (2019)
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[Synch] F. Arrigoni and T. Pajdla Motion segmentation via synchronization ICCV Workshops (2019)

## Conclusion

- We presented a novel solution to motion segmentation with two-frame correspondences, which is a poorly studied task.
- Differently from previous works considering the same assumptions, our approach can handle an unknown number of motions, hence it is more general and practical.
- Our method achieves comparable or better accuracy than its competitors on existing datasets, while correctly estimating the number of moving objects in every scene.

Thank you for your attention!

