



# Constructing Geographic and Long-term Temporal Graph for Traffic Forecasting

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# Background of Traffic Forecasting & GLT

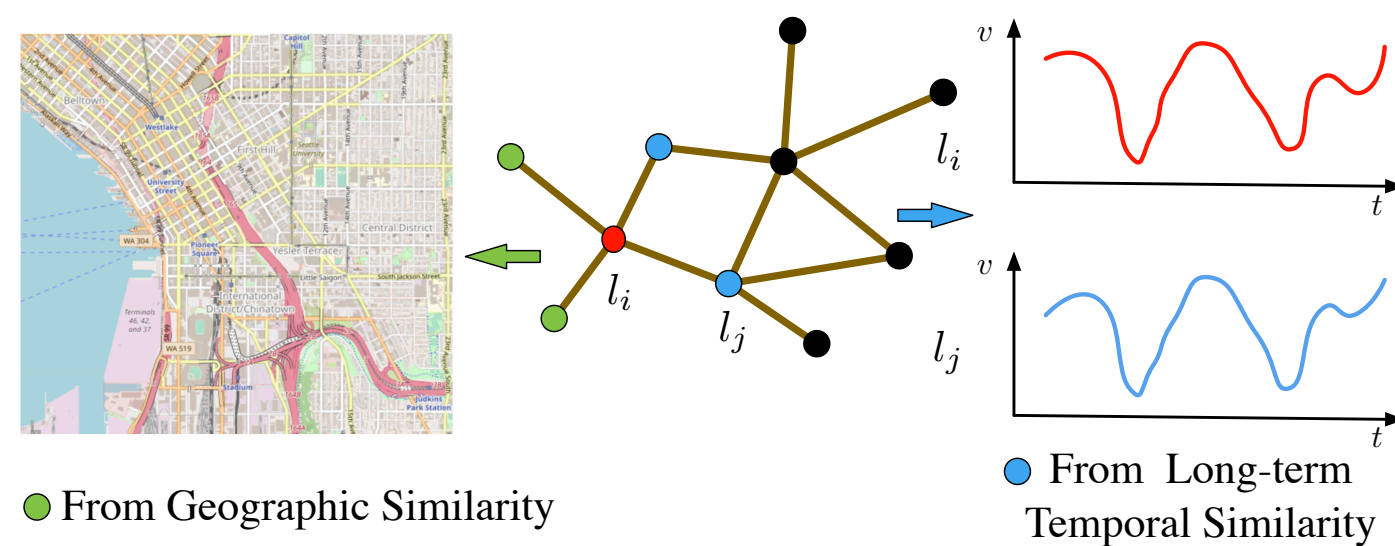


Fig.1. The conceptual demonstration of the construction process of Geographic and Long-term Temporal (GLT) Graph.

- Traffic forecasting: predicting future traffic states of road segments given sequential historical traffic states and the road network.
- Recent SOTA: GCN  $\rightarrow$  spatial; RNN  $\rightarrow$  temporal.
- The graph **only** based on the geographic information.
- Geographic and Long-term Temporal (GLT) Graph.
- GLT-GCRNN: the first deep learning framework which considers **both** the geographic and long-term temporal information.

# Constructing the GLT Graph

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- In the geographic aspect,

$$S_G^k = \min \left( (A + I)^k, 1 \right)$$

- In the long-term temporal aspect, the difference matrix  $Q$ .

$$Q_{ij} = Q_{ji} = \|\hat{\mathbf{v}}(i) - \hat{\mathbf{v}}(j)\|_2$$

- The similar matrix in the long-term temporal aspect.

$$S_{LT} = \begin{cases} 1, & Q_{i,j} \in Q_{i,:} \text{ top } \gamma \text{ small elements} \\ 0, & \text{otherwise} \end{cases}$$

- The k-hop geographic and long-term temporal similar matrix:

$$S_{GLT}^k = S_G^k + S_{LT}$$

# Constructing the GLT Graph

- Two representative groups of long-term temporal similar links,

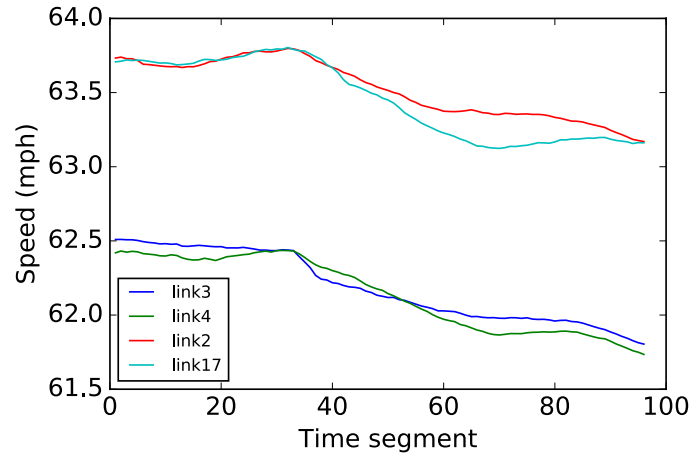


Fig.2. Two representative groups of long term temporal similar links.

Link 2 is the most LT similar link of link 17, nevertheless, they are not geographic similar which is **ignored** by  $S_G$ .

$S_{LT} \rightarrow$  let them **interact**.

- The free-flow reachable matrix is also adopted:

$$S_{Fi,j} = \begin{cases} 1, & V_{i,j}m\Delta t \geq D_{i,j} \\ 0, & \text{otherwise} \end{cases}$$

- The k-hop ultimate similar matrix :

$$S_U^k = S_{GLT}^k \odot S_F$$

# GLT Graph Convolution and Modified LSTM

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- GLT graph convolution operation

$$\mathbf{g}_t^k = \left( \mathbf{W}_g^k \odot \mathbf{S}_U^k \right) \mathbf{x}_t$$

- $\mathbf{g}_t^k$  extracted according to various hops are concatenated:

$$\mathbf{G}_t^K = [\mathbf{g}_t^1, \mathbf{g}_t^2, \dots, \mathbf{g}_t^K]$$

- The cell state gate is also modified:

$$\mathbf{C}_{t-1}^* = \mathbf{W}_C \odot \mathbf{S}_U^K \cdot \mathbf{C}_{t-1}$$

# Overall Framework of GLT-GCRNN

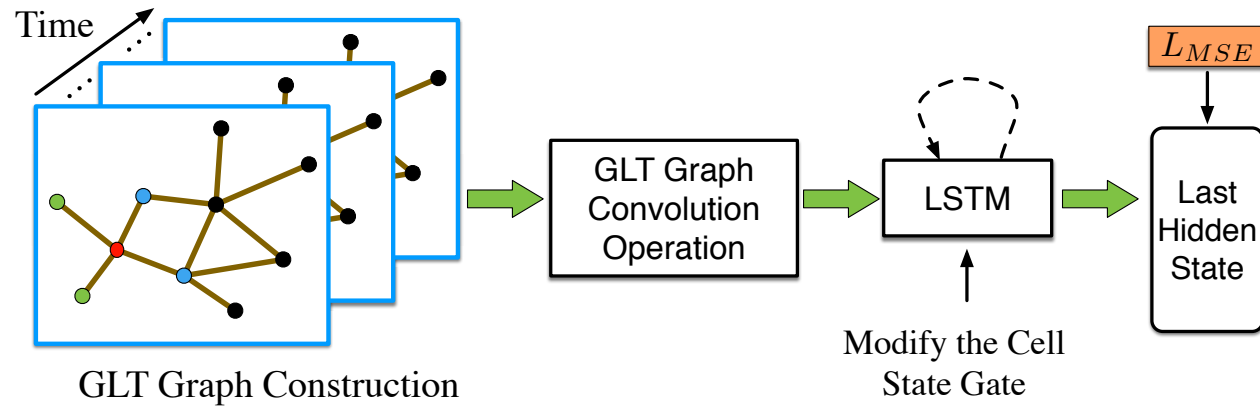


Fig.3. The overall framework of GLT-GCRNN.

- (1) The GLT graph construction.
- (2) GLT graph convolution operation for mining the spatial correlation.
- (3) Modified LSTM to capture the time series dependency.

The objective function:

$$L_{MSE} = \frac{1}{n} \sum_{i=1}^n (y_i - y'_i)^2$$

# Dataset & Evaluation Metrics

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TABLE I  
STATISTICS OF THE REAL-WORLD TRAFFIC FORECASTING DATASET

location	time span	# sensor	interval
Greater Seattle Area	1 year (2015)	323	5-minute

Rooted Mean Square Error:

$$\text{RMSE} = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - y'_i)^2}$$

Mean Absolute Percentage Error:

$$\text{MAPE} = \frac{1}{n} \sum_{i=1}^n \frac{|y_i - y'_i|}{y_i}$$

Mean Absolute Error:

$$\text{MAE} = \frac{1}{n} \sum_{i=1}^n |y_i - y'_i|$$

# Experimental results

TABLE II  
TRAFFIC FORECASTING RESULT COMPARISON ON THE NETWORK-SCALE  
DATASET

	RMSE (mph)	MAPE (%)	MAE (mph)
ARIMA	10.65	13.85	6.10
SVR	11.12	14.39	6.85
FNN	7.83	10.19	4.45
LSTM	4.97	6.83	2.70
DiffGRU	8.22	11.18	4.64
Conv+LSTM	5.02	6.79	2.71
SGC+LSTM	4.80	6.52	2.64
LSGC+LSTM	6.18	7.51	3.16
TGC-LSTM	4.63	6.01	2.57
<i>GLT-GCRNN</i> (ours)	<b>3.59</b>	<b>5.90</b>	<b>2.45</b>

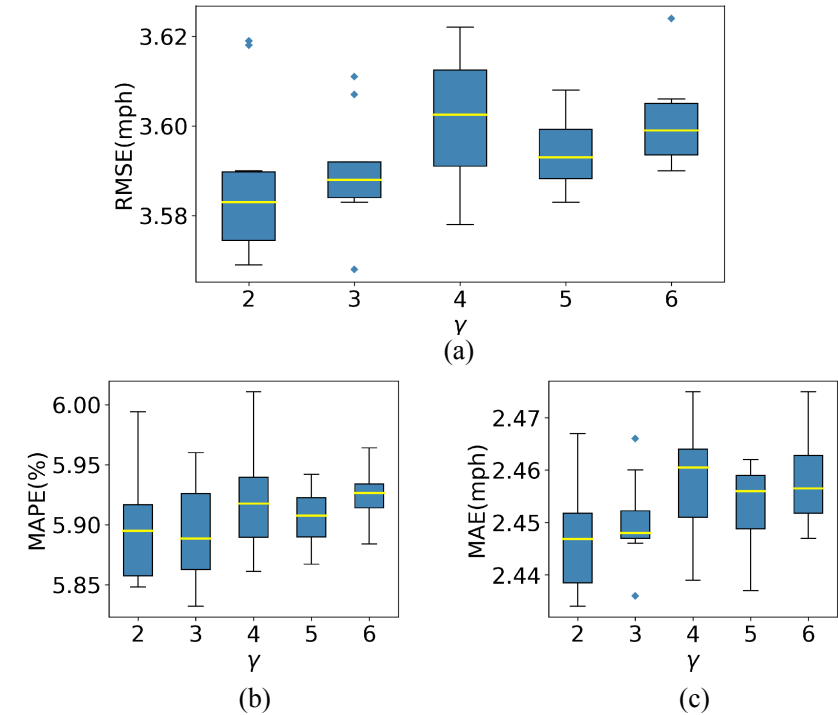


Fig.4. The influence of hyper-parameter  $\gamma$ : (a) Regarding to RMSE. (b) Regarding to MAPE. (c) Regarding to MAE.



# Experimental results

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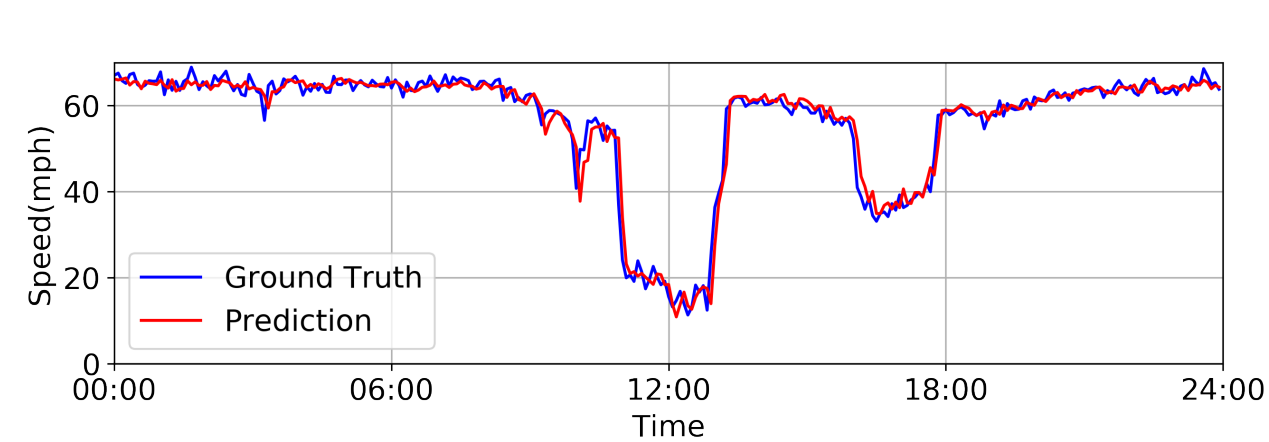


Fig.5. The traffic forecasting visualization of GLT-GCRNN. The link's ID is 190 and the date is 2015-12-27.

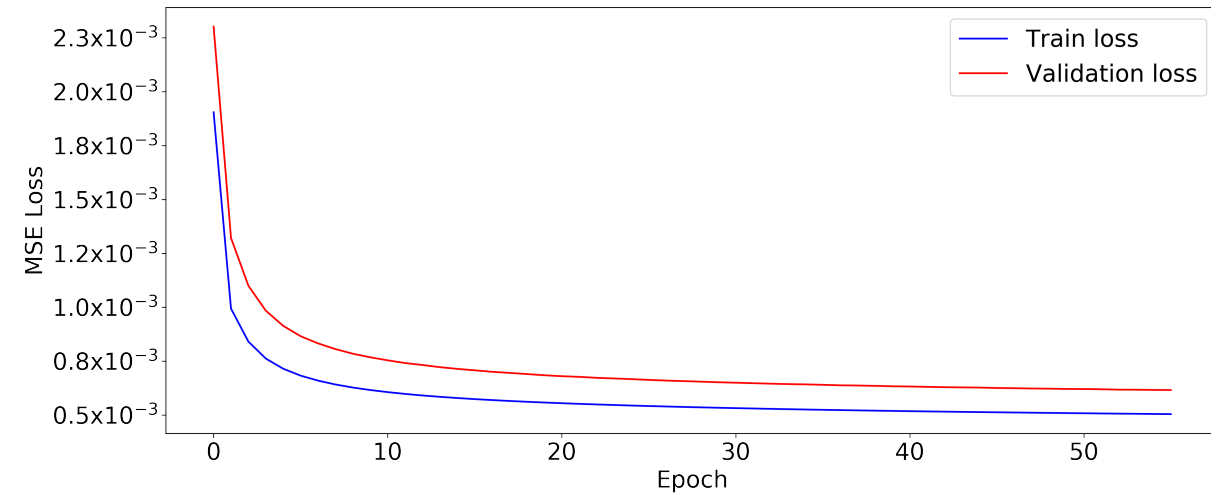


Fig.6. The training and validation process of GLT-GCRNN.

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Thank you for listening.

