

# Adaptive Noise Injection for Training Stochastic Student Networks from Deterministic Teachers

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# Background - Preamble

- Machine learning models are widely used to automate decision making processes
  - E.g. image classification



# Background - Preamble

- However, such methods are known to be susceptible to adversarial attacks.



“Otter”

+ Specially  
crafted  
perturbation →



“Monkey”

*Simple illustration of the effects of an adversarial attack*

# Background – Attacks Routines Used

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- We used several popular white-box attack routines
  1. Basic Iterative Method (BIM)
  2. Projected Gradient Descent (PGD)
  3. Momentum Iterative Method (MIM)
  4. Carlini & Wagner Attack (CW)
- A black-box attack routine was also used
  1. Boundary Attack (BA)

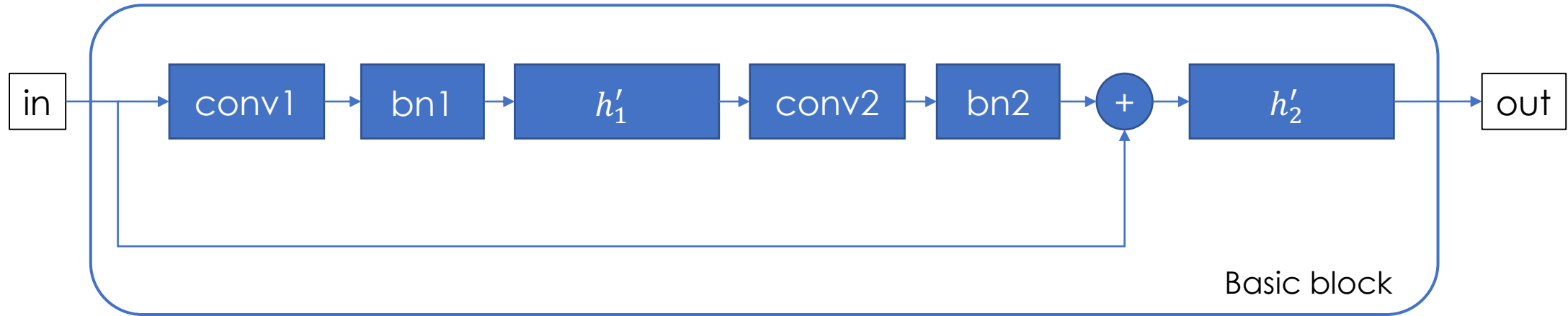
# Proposed Method

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- Propose Adaptive Noise Injection Stochastic Students ( $ANIS^2$ ) mechanism
  - Fine-tunes a deterministic network (teacher) to a stochastic variant (student)
  - Injects noise within *activation functions* with adaptive *stochasticity* during training
  - Using input data statistics based on Exponential Moving Average (EMA)
- *Different degrees of noise* are used at *different parts* of the network
  - Different hidden activation values across the network
- Trained in conjunction with Adversarial Training

# Proposed Method

- Denote our proposed activation block as StocReLUEMA,  $h'(\cdot)$
- For an exemplary ResNet18 basic block:



# Proposed Method

- Let our StocReLUEMA be  $h'(\cdot)$  and vanilla ReLU be  $h(\cdot)$ . At Layer  $i$ :

$$h'(x^{(i)}) = h(x^{(i)} + \delta^{(i)})$$

*such that  $\delta^{(i)} \sim N(0, \gamma \cdot \sigma^{(i)^2})$*

- $\gamma$  increases as training epochs increases
- Adaptive noise injection tuned during training, updated after each batch  $t$  via:

$$\sigma_{t+1}^{(i)} = (1 - \alpha) \cdot \sigma_t^{(i)} + \alpha \cdot STD_{chnwise}(x^{(i)})$$

# Proposed Method

- $\alpha$  set as 0.5
- Recall that StocReLUEMA:

$$h'(x^{(i)}) = h(x^{(i)} + \delta^{(i)})$$

such that  $\delta^{(i)} \sim N(0, \gamma \cdot \sigma^{(i)2})$

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**Algorithm 1:** Training with adaptive noise injector

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**Input:** Teacher network's weights,  $\theta_{teach}$ ; Max epochs,  $T$ ; Initial  $\gamma_{init}$ ; Max  $\gamma_{max}$ ; Gamma update interval,  $r$

**Output:** Student network's weights,  $\theta_{student}$   
Initialise stochastic student network with  $\theta_{teach}$  and

$\gamma_{init}$ ;  
 $k = r * (\gamma_{max} - \gamma_{init}) / T$ ;  
**for**  $t = 1, \dots, T$  **do**  
    Get mini-batch from training data  
     $B = \{(x_1, y_1), \dots, (x_m, y_m)\}$ ;  
    **for**  $j = 1, \dots, m$  **do**  
        Perform standard training routine with adversarial training on mini-batch;  
        Update  $\sigma$  in each stochastic layer,  
         $\sigma_{new} = (1 - \alpha) * \sigma_{old} + \alpha * STD_{chnwise}(input)$   
    **end**  
    **if**  $t \bmod r = 0$  **then**  
         $\gamma = \gamma + k$   
    **end**  
**end**

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# Baselines Used

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1. Adversarial Training (AT)
  - Trains model on adversarial samples generated with correct labels
2. TRADES
  - Introduce a regularisation term that encourages adversarial robustness
3. Learn2Perturb (L2P)
  - Introducing noise parameters as learnable parameters for the network
  - Trained with AT

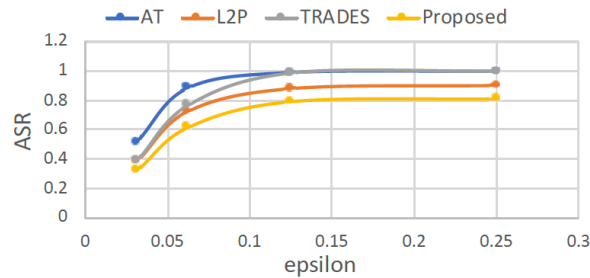
# Baseline Classification Results

Defence Methods	CIFAR-10	CIFAR-100
None	0.940	0.760
AT	0.846	0.574
L2P	0.859	0.566
TRADES	0.809	0.594
<b><i>ANIS<sup>2</sup> (Proposed)</i></b>	<b>0.829</b>	<b>0.575</b>

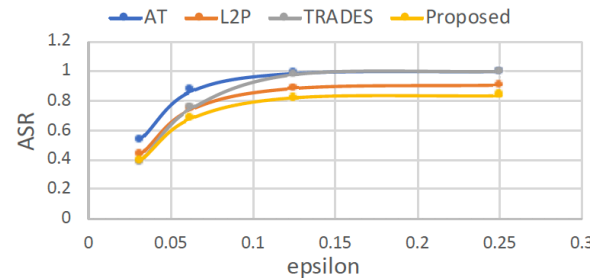
Classification accuracy of the respective approaches on clean CIFAR-10 and CIFAR-100 test data. “None” indicates standard training without any defence introduced. Higher is better.

# White-box Attack Results

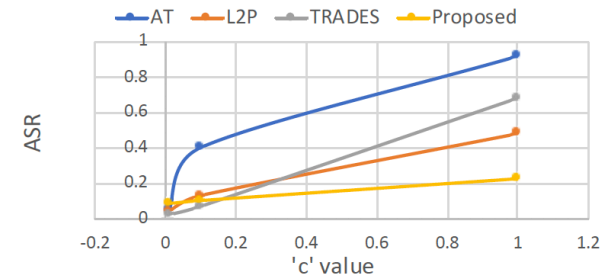
- We report the Adversarial Success Rate (ASR). More specifically:  
$$ASR = \mathbb{E}_{X,Y \sim D} \{P(f(x + \delta) \neq Y \mid f(x) = Y)\}$$



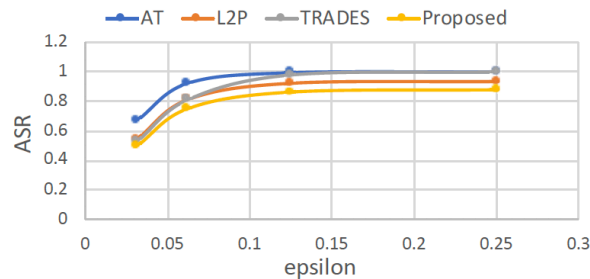
(a) BIM attack; CIFAR-10



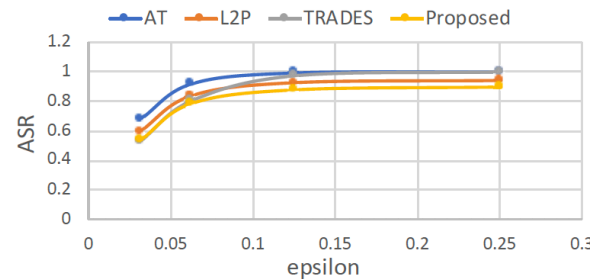
(b) MIM attack; CIFAR-10



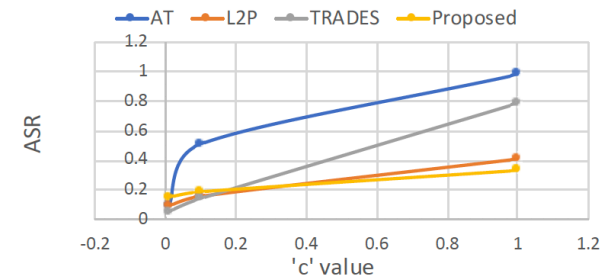
(c) CW attack; CIFAR-10



(d) BIM attack; CIFAR-100

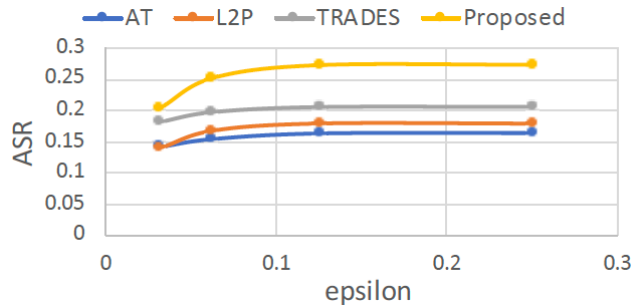


(e) MIM attack; CIFAR-100

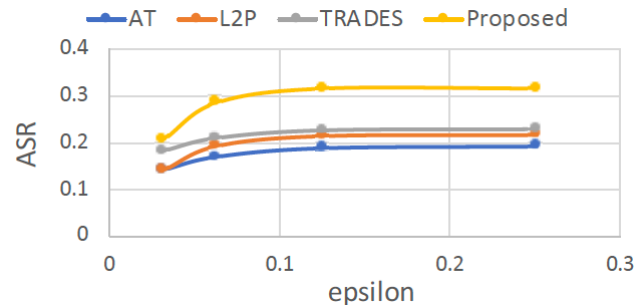


(f) CW attack; CIFAR-100

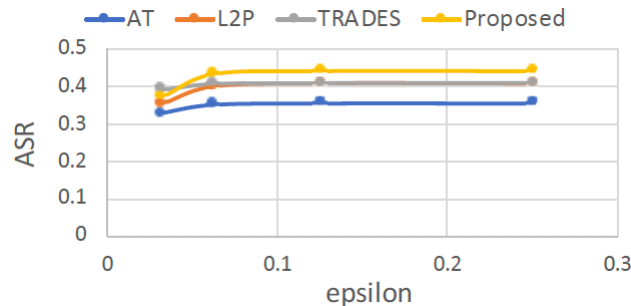
# Black-box Attack Results



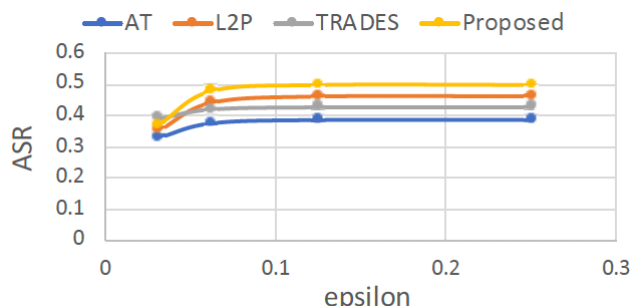
BIM attack on teacher model;  
CIFAR-10



MIM attack on teacher model;  
CIFAR-10



BIM attack on teacher model;  
CIFAR-100



MIM attack on teacher model;  
CIFAR-100

- Black-box *transferability* attack
  - Generate on teacher, launched against student
- Due to weights initialization policy
  - Proposed VS the rest

# Black-box Attack Results

- L2P and *ANIS*<sup>2</sup> show high robustness to decision-based black-box attacks

Defence Method	CIFAR-10	CIFAR-100
AT	0.758	0.818
L2P	<b>0.022</b>	<b>0.036</b>
TRADES	0.942	0.768
<i>ANIS</i> <sup>2</sup> (Proposed)	<b>0.048</b>	<b>0.064</b>

ASR against the various defence methods when launching BA across CIFAR-10 and CIFAR-100. 500 samples were used. Lower is better.

# Decision Boundary Evolution During Training

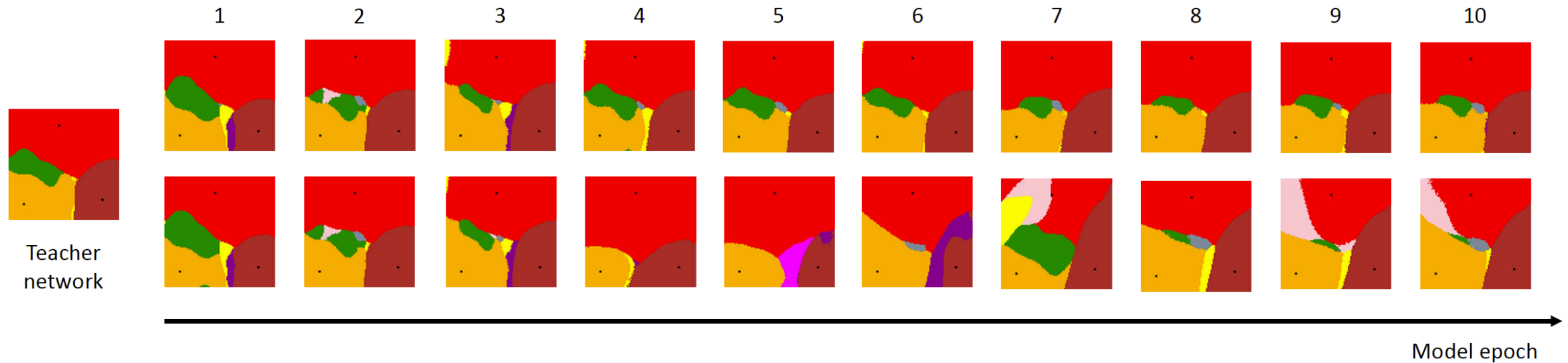
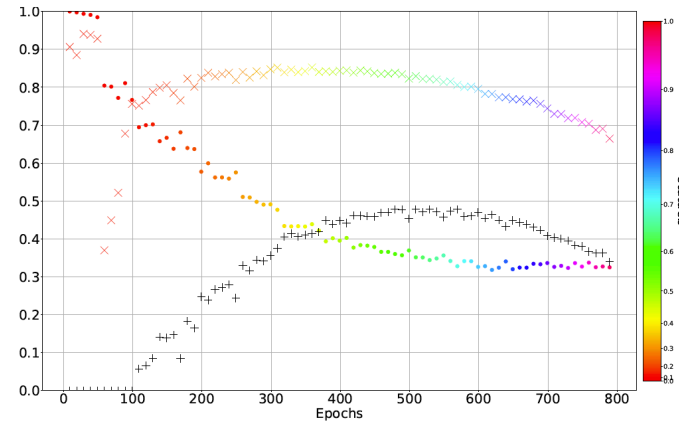


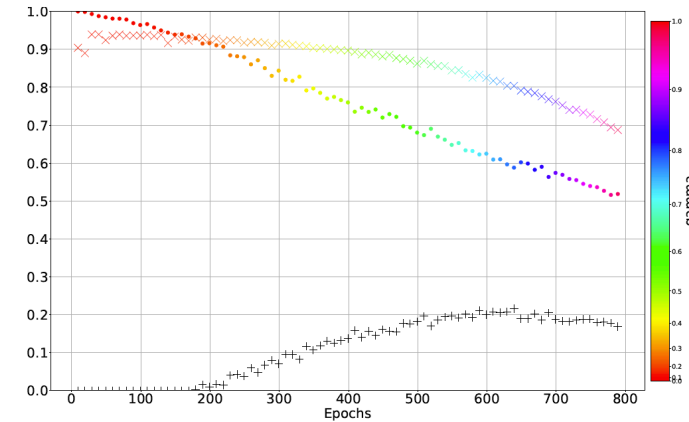
Illustration of prediction labels of an exemplary region based on three data points (black dots) of CIFAR-10. **Top row:** our stochastic student trained with *ANIS*<sup>2</sup> WITHOUT adversarial training. **Bottom row:** our stochastic student trained with *ANIS*<sup>2</sup> WITH adversarial training, introduced from the fourth image onward.

# Ablation Study

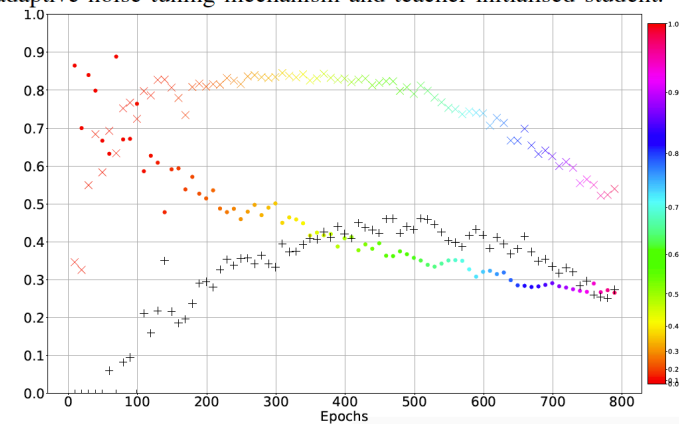
- Varied the following factors:
  - Presence of AT
  - Presence of EMA
  - Presence of teacher-initialisation
- Coloured 'x' – clean accuracy
- Coloured '.' – ASR
- Black '+' -  $\max(\text{ACC} - \text{ASR}, 0)$



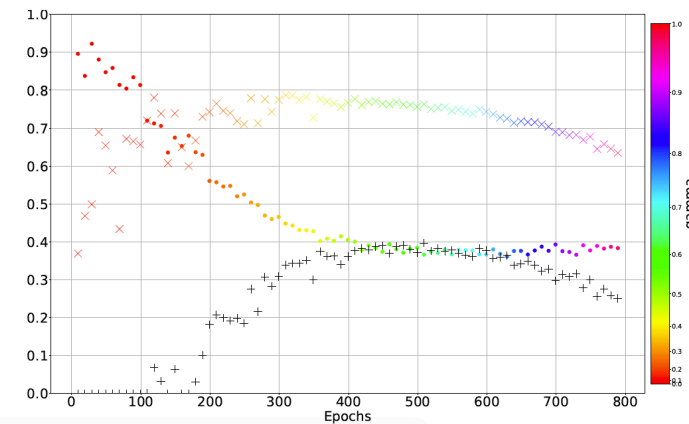
(a) Original proposed method with adversarial training, EMA-based adaptive noise tuning mechanism and teacher-initialised student.



(b) Without adversarial training.



(c) Without EMA-based adaptive noise tuning mechanism.



(d) Without teacher-initialisation of student.

# Conclusion

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- Propose *ANIS*<sup>2</sup>, conceptually simple EMA-based adaptive noise injection mechanism
  - Can be applied to any layer
- Able to outperform baselines in robustness under white-box attack settings
- AT as finetuning allows adaptation to new features
  - Exemplified by evolution of decision boundary
- EMA to adapt noise prevents sharp degradation in clean accuracy while providing smooth trends
- Stochasticity should be used as a complement instead of a substitute



# Selected References

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